



# NBS TECHNICAL NOTE 932

U.S. DEPARTMENT OF COMMERCE / National Bureau of Standards

## Concrete Strength During Construction

QC  
100  
.U5753  
No. 932  
1976  
c.2

# NATIONAL BUREAU OF STANDARDS

The National Bureau of Standards<sup>1</sup> was established by an act of Congress March 3, 1901. The Bureau's overall goal is to strengthen and advance the Nation's science and technology and facilitate their effective application for public benefit. To this end, the Bureau conducts research and provides: (1) a basis for the Nation's physical measurement system, (2) scientific and technological services for industry and government, (3) a technical basis for equity in trade, and (4) technical services to promote public safety. The Bureau consists of the Institute for Basic Standards, the Institute for Materials Research, the Institute for Applied Technology, the Institute for Computer Sciences and Technology, and the Office for Information Programs.

**THE INSTITUTE FOR BASIC STANDARDS** provides the central basis within the United States of a complete and consistent system of physical measurement; coordinates that system with measurement systems of other nations; and furnishes essential services leading to accurate and uniform physical measurements throughout the Nation's scientific community, industry, and commerce. The Institute consists of the Office of Measurement Services, the Office of Radiation Measurement and the following Center and divisions:

Applied Mathematics — Electricity — Mechanics — Heat — Optical Physics — Center for Radiation Research: Nuclear Sciences; Applied Radiation — Laboratory Astrophysics<sup>2</sup> — Cryogenics<sup>2</sup> — Electromagnetics<sup>2</sup> — Time and Frequency<sup>2</sup>.

**THE INSTITUTE FOR MATERIALS RESEARCH** conducts materials research leading to improved methods of measurement, standards, and data on the properties of well-characterized materials needed by industry, commerce, educational institutions, and Government; provides advisory and research services to other Government agencies; and develops, produces, and distributes standard reference materials. The Institute consists of the Office of Standard Reference Materials, the Office of Air and Water Measurement, and the following divisions:

Analytical Chemistry — Polymers — Metallurgy — Inorganic Materials — Reactor Radiation — Physical Chemistry.

**THE INSTITUTE FOR APPLIED TECHNOLOGY** provides technical services to promote the use of available technology and to facilitate technological innovation in industry and Government; cooperates with public and private organizations leading to the development of technological standards (including mandatory safety standards), codes and methods of test; and provides technical advice and services to Government agencies upon request. The Institute consists of the following divisions and Centers:

Standards Application and Analysis — Electronic Technology — Center for Consumer Product Technology: Product Systems Analysis; Product Engineering — Center for Building Technology: Structures, Materials, and Life Safety; Building Environment; Technical Evaluation and Application — Center for Fire Research: Fire Science; Fire Safety Engineering.

**THE INSTITUTE FOR COMPUTER SCIENCES AND TECHNOLOGY** conducts research and provides technical services designed to aid Government agencies in improving cost effectiveness in the conduct of their programs through the selection, acquisition, and effective utilization of automatic data processing equipment; and serves as the principal focus within the executive branch for the development of Federal standards for automatic data processing equipment, techniques, and computer languages. The Institute consists of the following divisions:

Computer Services — Systems and Software — Computer Systems Engineering — Information Technology.

**THE OFFICE FOR INFORMATION PROGRAMS** promotes optimum dissemination and accessibility of scientific information generated within NBS and other agencies of the Federal Government; promotes the development of the National Standard Reference Data System and a system of information analysis centers dealing with the broader aspects of the National Measurement System; provides appropriate services to ensure that the NBS staff has optimum accessibility to the scientific information of the world. The Office consists of the following organizational units:

Office of Standard Reference Data — Office of Information Activities — Office of Technical Publications — Library — Office of International Relations — Office of International Standards.

<sup>1</sup> Headquarters and Laboratories at Gaithersburg, Maryland, unless otherwise noted; mailing address Washington, D.C. 20234.

<sup>2</sup> Located at Boulder, Colorado 80302.

30 1976

cc. ref

# Concrete Strength During Construction

Technical Note, No. 30

753  
932  
76  
2

H. S. Lew, T. W. Reichard, and  
J. R. Clifton

Center for Building Technology  
Institute for Applied Technology  
National Bureau of Standards  
Washington, D.C. 20234



---

U.S. DEPARTMENT OF COMMERCE, Elliot L. Richardson, Secretary

Edward O. Vetter, Under Secretary

Dr. Betsy Ancker-Johnson, Assistant Secretary for Science and Technology

NATIONAL BUREAU OF STANDARDS, Ernest Ambler, Acting Director

Issued December 1976

National Bureau of Standards Technical Note 932

Nat. Bur. Stand. (U.S.), Tech. Note 932, 56 pages (Dec. 1976)

CODEN: NBTNAE

U.S. GOVERNMENT PRINTING OFFICE  
WASHINGTON: 1976

---

For sale by the Superintendent of Documents, U.S. Government Printing Office, Washington, D.C. 20402  
(Order by SD Catalog No. C13.46:932). Stock No. 003-003-017-03-5 Price \$1.35  
(Add 25 percent additional for other than U.S. mailing).

CONTENTS

	Page
LIST OF FIGURES . . . . .	iv
LIST OF TABLES . . . . .	v
LIST OF SYMBOLS . . . . .	vi
Abstract . . . . .	1
1. INTRODUCTION . . . . .	2
1.1 Background and Purpose. . . . .	2
1.2 Scope . . . . .	3
2. DESCRIPTION OF TESTS . . . . .	4
2.1 Preparation of Test Specimens . . . . .	4
2.1.1 Description of Test Specimens. . . . .	4
2.1.2 Concrete . . . . .	4
2.2 Curing Procedure. . . . .	5
2.3 Test Procedure. . . . .	5
2.3.1 General. . . . .	5
2.3.2 Compressive Strength Test. . . . .	5
2.3.3 Splitting Tensile Strength Test. . . . .	6
2.3.4 Pull-Out Bond Strength Test. . . . .	6
2.3.5 Probe Penetration Test . . . . .	7
2.3.6 Rebound Hammer Test. . . . .	7
3. TEST RESULTS AND DISCUSSION. . . . .	8
3.1 General . . . . .	8
3.2 Maturity of Concrete. . . . .	9
3.3 Compressive Strength Test . . . . .	9
3.4 Modulus of Elasticity . . . . .	11
3.5 Splitting Tensile Strength Test . . . . .	12
3.6 Pull-Out Bond Strength Test . . . . .	12
3.7 Rate of Strength and Modulus Gain with Maturity . . . . .	13
3.8 Non-Destructive Tests . . . . .	14
3.8.1 Probe Penetration. . . . .	14
3.8.2 Rebound Hammer . . . . .	15
4. SUMMARY AND CONCLUSIONS. . . . .	15
5. REFERENCES . . . . .	17

LIST OF FIGURES

	Page
Figure 1. Section Through Pull-out Specimen Rack and Mold . . . . .	29
Figure 2. Compressive Test of Cylinder. . . . .	30
Figure 3. Splitting Tensile Test of Cylinder. . . . .	31
Figure 4. Pull-out Test Setup . . . . .	32
Figure 5. Pull-out Bond Test. . . . .	33
Figure 6. Probe Penetration Test. . . . .	34
Figure 7. A Device Used to Measure the Average Penetration of Three Probes. . . . .	35
Figure 8. Rebound Hammer Test . . . . .	36
Figure 9. Cylinder Temperatures During Curing Period. . . . .	37
Figure 10. Compressive Strength Versus Maturity. . . . .	38
Figure 11. The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Compressive Strength Versus Maturity. . . . .	39
Figure 12. Typical Stress-Strain Curves of Compressive Tests of Cylinders Cured at 35 °F (1.7 °C) . . . . .	40
Figure 13. Secant Modulus Versus Maturity. . . . .	41
Figure 14. The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Secant Modulus Versus Maturity. . . . .	42
Figure 15. Splitting Tensile Strength Versus Maturity. . . . .	43
Figure 16. The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Splitting Tensile Strength Versus Maturity. . . . .	44
Figure 17. Pull-out Load Versus Maturity . . . . .	45
Figure 18. The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Pull-out Load Versus Maturity . . . . .	46
Figure 19. Normalized Mechanical Properties With Respect to 28-Day Values Versus Maturity . . . . .	47
Figure 20. Comparison of Measured Compressive Strength Versus Compressive Strength from Probe Chart . . . . .	48

LIST OF TABLES

	Page
Table 1. Distribution of Test Specimens to Three Curing Conditions. . .	20
Table 2. Compressive Strength Test Results. . . . .	21
Table 3. Splitting Tensile Strength Test Results. . . . .	22
Table 4. Pull-Out Bond Strength Test Results . . . . .	23
Table 5. Probe Penetration Test Results . . . . .	24
Table 6. Rebound Hammer Test Results. . . . .	25
Table 7. Mean Temperature of Concrete During Each Age Interval. . . . .	26
Table 8. Maturity Value of Concrete . . . . .	27
Table 9. Statistical Properties Associated with the Regression Equations. . . . .	28

## LIST OF SYMBOLS

$a$	=	Regression coefficient
$b$	=	Regression coefficient
$E_{si}$	=	Secant modulus of elasticity
$E_s$	=	28-day secant modulus of elasticity of concrete cured at 73 °F (22.8 °C)
$f'_c$	=	28-day compressive strength of concrete cured at 73 °F (22.8 °C)
$f'_{ci}$	=	Compressive strength of concrete other than $f'_c$
$f'_{sp}$	=	28-day splitting tensile strength of concrete cured at 73 °F (22.8 °C)
$f'_{spi}$	=	Splitting tensile strength of concrete other than $f'_{sp}$
$M$	=	Maturity of concrete
$P$	=	Probe penetration reading
$P_i$	=	Maximum pull-out load
$P'$	=	28-day maximum pull-out load of specimen cured at 73 °F (22.8 °C)
$r$	=	Coefficient of correlation
$r^2$	=	Coefficient of determination
$R$	=	Rebound number
$\bar{S}$	=	Sample standard deviation from regression
$S_a$	=	Standard error of regression coefficient $a$
$S_b$	=	Standard error of regression coefficient $b$
$T$	=	Temperature of concrete in degree Fahrenheit
$T_o$	=	Datum temperature of concrete in degree Fahrenheit
$\Delta t$	=	Increment of time in days
$\chi^2$	=	Chi-square statistic



## CONCRETE STRENGTH DURING CONSTRUCTION

H. S. Lew, T. W. Reichard and J. R. Clifton

The early strength gain characteristics of a concrete at various temperatures was investigated in this study. In addition, the applicability of two widely known non-destructive evaluation methods were examined for the purpose of determining the compressive strength of concrete at early ages.

For destructive evaluation, standard cylinder compression tests, splitting tensile tests and pull-out tests were made on specimens cured at 73 °F (22.8 °C), 55 °F (12.8 °C) and 35 °F (1.7 °C). For non-destructive evaluation, both probe penetration and rebound hammer tests were performed on slabs. Tests were carried out at the age of 1, 2, 3, 5, 7, 14, 28 and 42 days after casting the concrete.

Statistical analyses were made to examine the possibility of using maturity of concrete as a parameter to correlate test results of concrete cured at different temperatures. Rate of gain of the splitting tensile strength, pull-out bond strength and elastic modulus were compared with that of compressive strength.

The results show that when related to maturity, the rate of increase in the splitting tensile strength is about the same as that of the compressive strength, whereas the rate of increase in the pull-out strength and the modulus are slightly greater than that of the compressive strength. The results of non-destructive evaluations revealed that the compressive strength could not be estimated correctly by the probe method using the manufacturer's conversion charts. Because of lower rebound readings, the rebound hammer could not be used to estimate the compressive strength at early ages.

Key words: Compressive strength; concrete; maturity; mechanical properties; non-destructive evaluation; pull-out strength; splitting tensile strength.

## 1. INTRODUCTION

### 1.1 Background and Purpose

In recent years there have been a number of failures of large concrete structures [1,2]<sup>1</sup> during construction. Although the specific factors which triggered the failures may have been different, the main reason for the failures was the inadequacy, or absence of shoring necessary to support the partially matured concrete structure. The decision as to when shores and/or forms can be removed safely and how many levels of previously cast floors need to be reshored to support construction loads is based primarily on the rate of strength gain in the concrete and/or on the determination of in-situ strength of concrete.

Considerable information exists on the development of the compressive strength of concrete [3,4] under varying temperature and moisture conditions. These investigations have shown that the compressive strength can generally be predicted if the curing history, in terms of temperature, moisture and age, is known. However, the strength of flexural members such as beams and slabs are often governed by either shear (diagonal tension) or bond strength at early ages. It is usually assumed that these strength parameters are related to some function of the compressive strength [5,6]. The most common assumption is that they vary with the square root of the compressive strength. To date, no systematic investigation has been made to substantiate this functional relationship at early ages. Accordingly, one objective of this investigation was to determine the interrelationships between the compressive-strength gain of concrete with its strength gain in shear and bond and with the increase in modulus of elasticity.

In-situ strength of concrete members is usually determined from results of compressive tests of job-cured cylinders. Investigations [7,8] have shown that the results from cylinder tests, even when cured at the job site, generally do not correlate consistently with the strength of structural members. This inconsistency stems primarily from the difference in curing conditions because of shape and massiveness of section.

---

<sup>1</sup>Numbers in brackets indicate references listed at the end of this report.

In order to overcome the difficulty of simulating curing conditions, test results of cores taken from structural members are sometimes used to determine the concrete strength of those members. The variability in test results for cores is significantly greater than for the cylinder test, however. In a series of cylinder and core tests [7], the coefficient of variation for 216 core tests was 3.9 percent and for 216 cylinder tests was 2.4 percent. This shows that dispersion of core test results is greater than that of cylinder test results. The dispersion becomes greater as the number of tests becomes smaller. Because it is difficult and time consuming to mold, cure and test large numbers of cylinders or to remove cores, it would be desirable to have a reasonably accurate non-destructive test method for determination of the strength of concrete. Thus, the other objective of this investigation was to evaluate existing non-destructive evaluation (NDE) methods in determining the compressive strength of concrete at early ages. Two NDE methods, probe penetration (Windsor Probe)<sup>2</sup> and rebound hammer (Schmidt Hammer),<sup>2</sup> were evaluated in this study, and they are described in reference 9.

## 1.2 Scope

Since the purpose of this test series was to determine only the relative relationships between the several strength and stiffness properties of a specific concrete at early ages, the tests were designed to be as simple as possible. Three types of destructive tests and two types of non-destructive tests were performed. They are:

### Destructive Tests

1. Compressive strength test of cylindrical specimens
2. Splitting tensile strength test of cylindrical specimens
3. Bond strength test using cylindrical pull out specimens

### Non-destructive Tests

1. Probe-penetration test on slab specimens
2. Rebound-hammer test on slab specimens

---

<sup>2</sup>Proprietary names. These brand names are used merely to accurately identify the equipment used and their use does not imply an endorsement by the National Bureau of Standards.

All five types of tests were made on specimens cured at three different temperatures, 35 °F (1.7 °C), 55 °F (12.8 °C), and 73 °F (22.8 °C); and tested at nine ages, 1, 2, 3, 5, 7, 14, 21, 28 and 42 days.

## 2. DESCRIPTION OF TESTS

### 2.1 Preparation of Test Specimens

#### 2.1.1 Description of Test Specimens

Three types of concrete specimens were used. For the compressive and splitting tests, conventional 6 x 12 in (15 x 30 cm) cylinders were cast in waxed cardboard molds. For the NDE tests, unreinforced 3 ft x 5 ft x 5-1/2 in thick (0.915 m x 1.525 m x 140 mm) slabs were cast in oiled wood forms.

The pull-out specimens for the relative bond-strength tests consisted of a 48 in (1.2 m) long No. 6 (3/4 in or 19 mm) deformed reinforcing bar (62.3 ksi, or 429.6 MPa yield) cast in a 6 x 8 in (15 x 20 cm) waxed cardboard cylinder mold. Figure 1 shows the pull-out specimen and mold. The specimens were made so that the bar was bonded to the concrete for a length of 6 inches (15.2 cm) in all specimens. The pull-out molds were set up for casting in gang racks holding 6 specimens each. The racks were designed to rigidly hold each bar in a vertical position during the casting operation and during curing. The metal bottom of each cylinder mold had a hole drilled in it so that the bottom end of the bar would extend into a hole in the plywood base of the rack. A plastic furniture tip over the end of the bar sealed the hole in the bottom of the mold and protected the end of the bar. The concrete cylinder of each pull-out specimen was reinforced with a 4.5 in (11.4 cm) diameter cage made of 2 in x 2 in (5 cm x 5 cm) welded steel wire mesh of 16 gage (0.0625 in or 1.59 mm).

Table 1 lists the specimens cast and the temperatures at which they were cured.

#### 2.1.2 Concrete

The concrete was supplied by a local ready-mix company in a 3 yd<sup>3</sup> (2.3 m<sup>3</sup>) batch and was one of their standard mixes. The mix proportions for per cubic yard of concrete were:

517 lbs (235 kg)	Type I Cement
1365 lbs (619 kg)	Silica Sand
1750 lbs (794 kg)	Crushed Limestone (Maximum size, 3/4 in or 1.9 cm)
6 oz (170 g)	Air Entraining Agent

Water was added to provide a 3-1/2 in (8.9 cm) slump after 15 min of mixing. This mix resulted in a concrete containing 4-1/2 percent air and weighing 145.8 lb/ft<sup>3</sup> (2335 kg/m<sup>3</sup>) when placed. (Subsequently, the unit weight of the hardened concrete in the 6 x 12 in (15 x 30 cm) cylinders was determined to be 146.3 lb/ft<sup>3</sup> (2343 kg/m<sup>3</sup>). A total of 2 hours was required to mix and place the concrete. Internal vibration was used to consolidate the concrete in the slabs and 6 x 12 in (15 x 30 cm) cylinders. Rodding was used for the pull-out specimens. It should be noted that loss in slump was experienced because of the extended period required to place the test specimens.

## 2.2 Curing Procedures

The pull-out specimens and the NDE slabs were cast in the curing chambers which were temperature controlled. The compressive and splitting tensile test specimens were cast at a central location and then distributed to the curing chambers. Because humidities within the chambers were uncontrolled, the specimens were covered with polyethylene film to retard loss of moisture except for six pull-out specimens in each chamber which were sealed by seating steel capping plates on top of the fresh concrete. These "capped" specimens were tested when the concrete was 1 and 2 days old.

The nominal temperatures within the three chambers were 73 °F (22.8 °C), 55 °F (12.8 °C) and 35 °F (1.7 °C). The actual temperatures of the chambers and of the concrete within the chamber were recorded periodically. The temperature of the concrete was measured with a thermocouple cast in a 6 x 12 in (15 x 30 cm) cylinder stored in each chamber. All specimens were stored in the chambers until each test day.

## 2.3 Test Procedures

### 2.3.1 General

Three specimens from each curing condition were tested for each destructive test on scheduled test dates. The capping and testing of the cylinder specimens were done in a 70 °F (21 °C) environment.

### 2.3.2 Compressive Strength Test

For tests prior to 7 days each compressive test specimen was capped with a sulphur-silica compound at least one hour before test. For the 7-day and later tests the specimens were capped at least 2 days prior to test. After capping, these specimens were returned to the curing chamber and placed in plastic bags.

The compressive tests were performed in a hydraulic testing machine essentially as described by ASTM C39-72 [10]. The rate of loading was adjusted to be approximately 1/3 of the expected maximum load per minute. Figure 2 shows the compressive test setup.

Deformation of each specimen was measured during the compressive tests over a gage length of 8 inches (20.3 cm) with a compressometer such as is described in ASTM C 469-65 [10]. The output from a linear variable differential transformer (LVDT) mounted on the compressometer was recorded on the "x" axis of an x-y plotter and the load was recorded on the "y" axis.

### 2.3.3 Splitting Tensile Strength Test

The splitting test was performed in accordance with ASTM C 496-71 [10] except that the loading rate was adjusted to be approximately 1/4 of the expected maximum load per minute. Figure 3 shows the splitting test setup.

### 2.3.4 Pull-out Bond Strength Test

The testing procedure for the pull-out tests was essentially as described in ASTM C 234 [10] except that only the slip of the bar at the free end was measured. Figure 4 depicts the test setup. The load was applied in a screw-type testing machine at approximately 1/3 of the expected maximum load per minute. Loading was continued until resistance to pull-out decreased.

The load and free-end slip were recorded on an x-y recorder. The slip was measured with an LVDT which was mounted on a tripod held to the top of the specimen with hot-melt glue. Figure 5 shows a specimen under test.

It should be noted that the strength of the bond between reinforcing steel and concrete is a rather nebulous property in that there is no standard method for measurement of this property [11]. ASTM C 234-71 is a standard method used for comparing the "bond strengths" developed between a reinforcing steel bar and various concretes, but the values measured are not accepted as being design values [24]. For the purposes of this investigation it was assumed that a method based on ASTM C 234-71 can be used to determine the relative values of bond strength between No. 6 deformed bars and a concrete at the various ages and cure conditions.

### 2.3.5 Probe Penetration Test

This procedure [9] is based on the depth of penetration of a special steel probe when driven into concrete with a precisely controlled powder charge. Empirically-obtained relationships are used to determine the compressive strength in terms of penetration measurements. The probes, powder charges (32 caliber blank cartridges), special driving gun, templates for guiding the probes, and a special measuring device are all part of a proprietary system available from the manufacturer. The measurements used are actually the converse of the depth-of-penetration, i.e., exposed length of the probe.

The manufacturer supplies a set of 5 calibration curves, each curve corresponding to a specific Mohs' hardness value<sup>3</sup> for the coarse aggregate used in the concrete, by which penetration measurements can be converted to strength measurements. However, several investigators have observed [11,12,13] that use of the manufacturer's calibration curve often results in grossly incorrect estimates of the compressive strength of concretes. These investigators recommend that the probe should be calibrated whenever the type of aggregate is changed.

For this investigation six probes were driven into each concrete slab (fig. 6) at each test age and the lengths of the probes extending above the concrete were measured using both a steel rule and the measuring device supplied by the manufacturer of the equipment (fig. 7). The Mohs' hardness value for the coarse aggregate was 5.

A low-power setting of the gun was used for testing at ages 1, 2 and 3 days for all concrete slabs, and at the age of 5 days for the slab cured at 55 °F. All other tests were performed using the standard power setting.

### 2.3.6 Rebound Hammer Test

This procedure [9] is a widely used method of estimating the compressive strength of concrete based on the distance a steel plunger rebounds from the concrete surface after a precisely controlled impact.

The rebound hammer consists of a steel plunger and a tension spring in a tubular frame (fig. 8). When the head of the hammer is pushed against the concrete surface, the steel plunger is retracted against the force of the spring. When the head is completely retracted, the spring is automatically

<sup>3</sup>Mohs' scale is an arbitrary mineralogical scale of hardness in which a mineral will scratch other minerals that are lower on the scale (smaller hardness number) and will in turn be scratched by minerals higher on the scale. The Mohs' hardness number ranges from 1 for a talc to 10 for a diamond.

released; the plunger is driven against the concrete and it rebounds. The rebound distance is indicated by a pointer on a scale that is graduated from 10 to 100, and the rebound readings are termed R-values.

Each hammer is furnished with a calibration chart supplied by the manufacturer, showing the relationship between compressive strength of concrete and rebound readings. This chart is based on data from tests conducted by the Swiss Federal Materials Testing and Experimental Institute. Each hammer, however, is known to vary slightly in performance.

### 3. TEST RESULTS AND DISCUSSION

#### 3.1 General

The two objectives of this phase of the investigation were to evaluate the feasibility of determining all the pertinent mechanical properties at early ages for a concrete cured at various temperatures when (1) either one strength parameter is known or (2) results from NDE tests are known.

Currently, two methods are widely used to determine in-place strength of concrete. With one method, the "present" strength and stiffness of members are estimated to be some ratio of the design values. The ratio is taken from an assumed relationship between compressive strength and age of the concrete. With the other method, the "present" strength and stiffness of members are estimated from compressive strength measurements made on either site-cured cylinders or on cores taken from representative members. Other pertinent mechanical properties are estimated from these measured values.

The basic test data for this phase of the work are presented in tables 2 through 6 and figure 9. These tables give the test data for the five types of tests and figure 9 indicates the temperature of the concrete at various ages during the curing period.

The initial temperature of the concrete was 80 °F (26.7 °C) as indicated in figure 9. It should be noted that the temperature control for the 35 °F (1.7 °C) chamber was erratic during the 17 to 30 day period. The sensitivity of the temperature measurements is estimated to be  $\pm 1$  °F (0.6 °C) for the 75 °F (22.8 °C) chamber and  $\pm 2$  °F (1.1 °C) for the other two chambers. Table 7 gives the mean temperature of the concrete for each relevant time interval during the curing period. The mean-temperature data was used in the following discussion of the maturity of concrete.



### 3.2 Maturity of Concrete

It is known that the strength of concrete increases with time and that the rate of increase is greatly affected by temperature of cure. The combined effect of temperature and time (maturity) on the gain of the strength of concrete has been investigated by others [12,13,14,15]. The term "maturity," usually expressed in "degree-day (or hour)," may be defined as the sum of the product of the increment of age of cure and the difference between curing and some temperature below which no strength gain takes place. The definition can be written as:

$$M = \Sigma (T-T_0) \Delta t \quad (1)$$

where T is temperature of the concrete at any time,  $T_0$  is a datum temperature below which no strength gain of concrete takes place, and  $\Delta t$  is the increment of time.

It has been shown from a series of compressive tests [12] that the strength of concrete remains constant at about 10 °F (-12.2 °C). Thus, equation (1) can be expressed as:

$$M = \Sigma (T-10) \Delta t \quad (\text{where } T \text{ is in } ^\circ\text{F}). \quad (2)$$

The values of M for each of the three curing conditions are listed in table 8.

### 3.3 Compressive Strength Test

Figure 10 is a semi-log plot of the compressive strength data (average of 3 specimens) versus the maturity of the concrete. Individual regression lines obtained by the method of least squares are shown for each curing temperature. Pertinent statistical properties associated with each regression equation are given in table 9. Judging from the residual standard deviation of the individual regression lines, the compressive strength of the concrete can be related adequately to the maturity for each curing temperature. A good correlation among lines also suggests the possibility of expressing all the data, regardless of the curing condition, by a single regression line. This line is also shown in figure 10. While the residual standard deviation of the all-data line is somewhat greater than that of the individual lines (215 vs 121, 163 and 108 in table 9), the data for all three cures fall reasonably well along the all-data line.

In order to examine whether all the test points can be treated as one population, individual regression lines are compared with each other in terms of statistical quantities. First, a comparison is made of residual variances of the data about their respective regression lines (test of homogeneity of variances); next, the slopes of the individual regression lines are compared; and finally, relative positions of individual regression lines (or intercepts) are compared.<sup>4</sup>

Homogeneity of the variances is tested by Bartlett's chi-square statistics [16]. The null hypothesis for the test is that individual variances are estimates of the same population variance. The computed value of chi-square statistic for the three lines was 1.20 with 2 degrees of freedom. When this value is compared with the theoretical chi-square distribution of 5.99 at a 5 percent significant level, the conclusion is to accept the null hypothesis. This is to say that the degree of dispersion of individual test points about their own regression line is about the same for all three lines.

Having established homogeneity of the residual variances, the slopes and intercepts are examined next. Any significant difference in individual slopes (b's) and intercepts (a's) is tested by comparing the ranges bound by the lower and upper limits of the slopes and intercepts of individual lines. The lower and upper limits are determined by computing confidence limits of the slopes and intercepts for a selected confidence coefficient. If these ranges overlap one another, it can be said that the slopes and intercepts do not differ significantly one another.

The lower and upper limits of the regression line  $f'_c = a + b \log M$  are expressed as:

$$a - tS_a, \quad a + tS_a$$

$$b - tS_b, \quad b + tS_b$$

for the value of t (t distribution) corresponding to the degrees of freedom and confidence coefficient [17]. In the above expressions  $S_a$  and  $S_b$  are the standard errors of estimate of the regression coefficients a and b, respectively (see table 9). At a significance level of 0.05 (confidence coefficient 0.95) and with the degrees of freedom associated with  $\bar{S}$ , the lower and upper limits for the intercepts and slopes are computed and graphically depicted in figure 11. It is seen that the ranges of both the intercepts and slopes of

<sup>4</sup>The slopes and intercepts are compared here separately for simplicity and a more rigorous method for comparing several regression lines is given in reference [16].

the 73 °F (22.8 °C) and 55 °F (12.8 °C) lines show overlap, while those of the 35 °F line do not overlap with those of the other two. This suggests that the trend of the compressive strength gain of the 35 °F (1.7 °C) cure specimens with time appears somewhat different from the other two. Since no definite conclusion can be drawn as to whether each regression line is significantly different from one another, there is no reason not to assume that the entire data are from a single population. The test of homogeneity of variance also supports the conclusion that the data from each individual group have the same characteristics. In light of the statistical evaluations, and the fact that the actual data fall fairly close to the all-data regression line (see fig. 10) the compressive strength of other concretes cured at different temperatures could be expressed in terms of maturity by a single line.

In the analysis of the other data presented in this report, the above described analytical procedures were followed to see whether the three regression lines from the three separate cures can be considered to be from a single population.

### 3.4 Modulus of Elasticity

The values of the modulus of elasticity listed in table 2 are the secant moduli of elasticity obtained at the stress levels  $0.4 f'_{ci}$  and  $0.8 f'_{ci}$  from stress-strain curves of the compressive test. Typical curves of the 35 °F (1.7 °C)-cure specimens are shown in figure 12. The characteristics of the stress-strain curves of specimens cured at 73 °F (22.8 °C) and 55 °F (12.8 °C) are similar to these curves.

In figure 13, the secant moduli are plotted against the maturity of the concrete. Regression lines are shown for each curing temperature. Pertinent statistical properties of these regression lines are listed in table 9. The procedures for statistical analyses as used in the case of the compressive strength were followed to see whether the data of three separate cures can be combined as a single group. Bartlett's chi-square statistic is 2.02 with 2 degrees of freedom. With the theoretical value of 5.99 at a 5 percent significant level, no significant difference in residual variances is expected among the three groups of the data. The lower and upper limits of the intercepts and slopes are depicted in figure 14. It is seen that the ranges of the slopes of the three curves all overlap one another, thereby indicating that the slopes of the curves are statistically about the same. However, in the case of the intercept, the range of the 35 °F (1.7 °C)-cure line lies apart from the other two. This seems to suggest that dissimilarity of this

group of data from the rest. However, the test on intercept being the weakest of the three tests, the hypothesis that the three regression lines are a family of lines of a single population cannot be rejected based solely on this test. Therefore, in this study, all three groups of data are treated as a single population.

### 3.5 Splitting Tensile Strength Test

A semi-log plot of the splitting tensile strength versus maturity is shown in figure 15. In general, the test points fall reasonably close to the all-data regression line. The dispersion of the data relative to the individual regression lines is about the same as that noted in the compressive strength versus maturity. The coefficients of determination are 0.97, 0.98 and 0.99 for the three regression lines, indicating a strong correlation between the two variables. This clearly shows that the splitting tensile strength can also be related to maturity as well as the compressive strength.

From figure 15 it is seen that the all-data line fits well through the entire data with a coefficient of determination of 0.95. As in the previous cases, homogeneity of the residual variances, the intercepts and the slopes of the three individual lines are compared to see whether the entire data, irrespective of curing temperature, can be treated collectively as a single group and represented by a single line. The analysis gives a Bartlett's chi-square of 5.46 (theoretical  $\chi^2 = 5.99$  at  $\alpha = 0.05$ ) with 2 degrees of freedom. As before, this test shows no significant difference in the three residual variances of the data of each temperature group about its own regression line, this confirming homogeneity of the data.

The ranges of the intercepts and slopes are shown in figure 16. The relative positions of the range of the limits show that only the intercept of the 35 °F (1.7 °C)-cure line does not overlap with the others. This can be attributed to a wider dispersal of the 35 °F (1.7 °C)-cure data compared with the others. These analyses, together with the actual distribution of the data shown in figure 15, indicate that the individual regression lines do not differ significantly one from the other and that the entire data could be represented by a single curve.

### 3.6 Pull-Out Bond Strength Tests

The pull-out test does not provide a realistic bond strength which can be used in design of flexural members. This is due primarily to the different

crack patterns between those developed in pull-out specimens and those in flexural specimens [25]. However, past research has shown that pull-out tests can be used satisfactorily to determine relative bond strengths [19,20]. Accordingly, pull-out tests were carried out in this investigation because the purpose of the investigation was to determine relative bond strength with respect to the 28-day strength.

A semi-log plot of the maximum pull-out loads versus maturity is shown in figure 17. In this figure those maximum loads governed by the yielding of the bar are shown as solid points. In the regression analyses these points are not included. Except for these solid points, the pull-out loads increased with maturity. As in other cases, the residual variances, the intercepts and the slopes of the individual lines are compared to determine if all the data can be treated as a single group.

A computed Bartlett's chi-square value is 1.17 (theoretical  $\chi^2 = 5.99$  at  $\alpha = 0.05$ ), with 2 degrees of freedom, indicating that the individual residual variances are not significantly different from one another. The lower and upper limits of the intercepts and slopes are shown in figure 18.

It is seen that the ranges of the intercept (a) and slope (b) of the 35 °F (1.7 °C)-cure line do not overlap with the ranges of the 55 °F (12.8 °C) - and 73 °F (22.8 °C)-cure lines. This disparity is also seen in figure 17 where the 35 °F (1.7 °C)-cure line has a steeper slope than the other two. Because the deviation of the 35 °F (1.7 °C) curve from the others could result from one or two extreme data points, the disparity of the intercept and slope alone could not be used as a reason for discriminating against the data of specimens cured at 35 °F (1.7 °C). More data are needed to reach a statistically valid conclusion. However, with narrowly dispersed data along the all-data line, together with a relatively small chi-square value in Bartlett's test, all the pull-out data are treated in this study as belonging to a single population.

### 3.7 Rate of Strength and Modulus Gain with Maturity

One of the purposes of this experimental study was to determine relative relationships between several important strength properties and the elastic modulus of a concrete at early ages. Inasmuch as the 28-day values of these mechanical properties obtained from a concrete cured at 73 °F (22.8 °C) have been accepted as a standard reference value, the compressive, splitting tensile and pull-out strengths and the moduli are normalized by dividing by their

respective 28-day value from 73 °F (22.8 °C) cure. These normalized values, when plotted against the maturity of concrete, can be used to compare the rate of increase in these strengths and the modulus with respect to the 28-day values. The least-square curves of the normalized plots for each of these strength properties and the modulus are shown in figure 19. Because the normalization was made with values obtained from the regression lines, the normalized curves do not pass through 1.0 at a maturity of 1764. For the concrete investigated in this study, the rate of increase in the splitting tensile strength is about the same as that of the compressive strength, whereas the rate of increase in the pull-out strength and the modulus are slightly greater than that of the compressive strength at early ages.

### 3.8 Non-Destructive Tests

#### 3.8.1 Probe Penetration

The averages, standard deviations, and coefficients of variation for the probe measurements are given in table 5. The average exposed lengths of probe were measured at 1 and 2 days using the mechanical averaging device (average of three probes). This averaging device is convenient to use, but it was desirable to determine the variation between individual penetrations. Thereafter, the exposed lengths of each probe were measured with a steel rule. The coefficient of variation for a set of either 5 or 6 measurements ranged from 2.6 to 13.7 percent, averaging 8.0 percent. Similar large variabilities in probe test results have been previously reported by Arni [21] and Malhotra [22]. Gaynor concluded [23] that the heterogeneity of concrete (with hardened cement past, mortar matrix and coarse aggregate phases) limits the accuracy of the probe system.

For each set of measurements, the compressive strength obtained from the cylinder test is plotted in figure 20 versus the strength predicted by the conversion chart provided by the probe manufacturer for the Mohs' hardness of 5. The solid points correspond to results using a low-charge setting and the open points correspond to results using the standard charge setting. Because the charts for the standard setting do not provide compressive strengths for low values of exposed probe length, 5- and 7-day readings of the 73 °F cure specimens, 7- and 14-day readings of the 55 °F cure specimens, 7, and 14 day readings of the 35 °F cure specimens are not included in the figure.

It is clearly evident from the figure that the probe readings overestimate considerably the cylinder strength. The difference between the strength predicted by the probe test and the cylinder test is greater at the

upper end of the chart for the low charge and the lower end of the chart for the standard charge. For Mohs' hardness value of 5, the compressive strength from the chart for the low charge ranges from 450 psi (3.10 MPa) to 4825 psi (29.55 MPa) and for the standard charge it ranges from 3050 psi (21.03 MPa) to 10,000 psi (68.95 MPa). Based on this investigation, it is reasonable to conclude that the probe method cannot be applied readily to all ages and types of concrete using the manufacturer's conversion charts to estimate the compressive strength.

### 3.8.2 Rebound Hammer

Fifteen rebound numbers were taken during each set of measurements and only the values above the minimum measurable level of 10 were used in calculating the averages, the standard deviations, and the coefficients of variation (table 6). In three instances, because of the large number of rebound values below 10, the averages were considered to be less than 10. The average compressive strength of cylinders cured at 55 °F (12.8 °C) and 35 °F (1.7 °C) ranged from 980 psi (6.76 MPa) to 1480 psi (10.21 MPa) for the first two days. Thus, for concretes having a compressive strength less than 1500 psi (10.34 MPa), rebound readings cannot be taken with certainty. Furthermore, for rebound readings less than 20 which is less than the lower 20% of the full scale of 100, the precision, thus the validity, of rebound measurements is questionable. In this investigation the coefficient of variation for a set of 15 measurements ranged from 6.2 to 20.5 percent. With these observations, no attempt is made to correlate the rebound readings to the compressive strength obtained from the cylinder test.

## 4. SUMMARY AND CONCLUSIONS

The gain in mechanical properties of a concrete with time was investigated in this study. In addition, two widely known non-destructive evaluation methods were examined as to their applicability in determination of the compressive strength of concrete at early ages. The test specimens cured at three temperatures were tested following three destructive and two non-destructive test procedures. The gain of splitting tensile and relative bond strengths and of the elastic modulus are compared with that of compressive strength. The compressive strength obtained from non-destructive evaluations are compared with the cylinder strength.

The following conclusions can be drawn from the test results:

- (1) Analysis of the test data shows that the compressive strength of concrete can be related to the maturity expressed in terms of concrete temperature and age of cure. Both a high value of the coefficient of determination of the all-data regression line and homogeneity of the residual variances of the individual regression lines indicate that the compressive strength data of a concrete cured at different temperatures could be treated collectively as a single group when expressed in terms of maturity.
- (2) When related to maturity, the elastic modulus data and the splitting tensile strength data of specimens cured at various temperatures could be treated as being from single groups.
- (3) The analysis of the results shows that the pull-out strength, when not governed by the yielding of the bar, could be expressed in terms of maturity, thus allowing the specimens cured at various temperatures to be treated as a single group. However, further investigation should be made with specimens cured at low temperatures to support the observation that the 35 °F (1.7 °C)-cure data deviated from the others.
- (4) At early ages, the rate of increase in the splitting tensile strength is about the same as that of the compressive strength, whereas the rate of increase in the pull-out strength and the modulus are slightly greater than that of the compressive strength.
- (5) It was found that for the concrete used in this investigation, the probe method did not estimate correctly the compressive strength when the estimation is made using the conversion charts provided by the manufacturer. Further tests are needed to ascertain the applicability of the probe method for estimation of the early strength of concrete.
- (6) Because of low rebound readings for concrete at early ages (below 20 percent of a full scale of 100), a reliable estimation of the compressive strength could not be made using the rebound hammer.



## 5. REFERENCES

- [1] "The Building Collapse at 2000 Commonwealth Avenue, Boston, Massachusetts," Report of the Mayor's Investigating Commission, City of Boston, Massachusetts, 1971.
- [2] Leyendecker, E. V. and Fattal, S. G., "Investigation of the Skyline Plaza Collapse in Fairfax County, Virginia," NBSIR 73-222, National Bureau of Standards, Washington, D.C., 1973.
- [3] Klieger, P., "Effect of Mixing and Curing Temperature on Concrete Strength," Journal of the American Concrete Institute, Vol. 54, American Concrete Institute, Detroit, Michigan, June 1958.
- [4] Price, W. H., "Factors Influencing Concrete Strength," Journal of the American Concrete Institute, Vol. 47, American Concrete Institute, Detroit, Michigan, February 1951.
- [5] Grundy, P. and Kabaila, A., "Construction Loads on Slabs With Shored Formwork in Multistory Buildings," Journal of the American Concrete Institute, Vol. 60, American Concrete Institute, Detroit, Michigan December 1963.
- [6] Agaswal, R. K. and Gardner, N. J., "Form and Shore Requirements for Multistory Flat Slab Type Buildings," Journal of the American Concrete Institute, Vol. 71, American Concrete Institute, Detroit, Michigan, November 1974.
- [7] Bloem, D. L., "Concrete Strength Measurements - Core Versus Cylinders," Proceedings of the American Society for Testing Material, Vol. 65, Philadelphia, Pa., 1965.
- [8] Bloem, D. L., "Concrete Strength in Structures," Journal of the American Concrete Institute, Vol. 65, American Concrete Institute, Detroit, Michigan, March 1968.
- [9] Clifton, J. R., "Nondestructive Tests to Determine Concrete Strength - A Status Report," NBSIR 75-729, National Bureau of Standards, Washington, D.C., 1975.
- [10] 1974 Annual Book of ASTM Standards, Part 14, American Society of Testing and Materials, Philadelphia, Pa., 19103.

- [11] "Bond Stress - The State of the Art," ACL Committee 408, American Concrete Institute, Detroit, Michigan, November 1966.
- [12] Plowman, J. M., "Maturity and the Strength of Concrete," Magazine of Concrete Research Vol. 8, No. 22, pp. 13-22, London, 1956.
- [13] Sadgrove, B. M., "Prediction of Strength Development in Concrete Structures," A paper presented at the 54th Annual Meeting of the Transportation Research Board, Washington, D.C., 1975.
- [14] Hudson, S. B. and Steele, G. W., "Prediction of Potential Strength of Concrete from the Results of Early Tests," Highway Research Record, No. 370, Highway Research Board, 1971.
- [15] Hudson, S. B. and Steele, G. W., "Developments in the Prediction of Potential Strength of Concrete from the Results of Early Test," A paper presented at the 54th Annual Meeting of the Transportation Research Board, Washington, D.C., 1975.
- [16] Snedecor, G. W. and Cochran, W. G., "Statistical Methods," 6th edition, The Iowa State University Press, Ames, Iowa, 1967.
- [17] Ku, H. H., "Statistical Concepts in Metrology," National Bureau of Standards Special Publication 300, Vol. 1, U.S. Government Printing Office, Washington, D.C. 20402, February 1969.
- [18] ACI 318-71, "Building Code Requirements for Reinforced Concrete," American Concrete Institute, Detroit, Michigan, 1971.
- [19] Bresler, B., editor, "Reinforced Concrete Engineering, Vol. I. Materials, Structural Elements Safety, Chapter 4," John Wiley & Sons, Inc., New York, 1974.
- [20] Ferguson, P. M., "Reinforced Concrete Fundamentals, Chapter 5," John Wiley & Sons, Inc., New York, 1971.
- [21] Arni, H. T., "Impact and Penetration Tests of Portland Cement Concrete in Nondestructive Testing of Concrete," Highway Research Record 378, pp. 55-67, Highway Research Board, 1972.
- [22] Malholtra, V. M. and Painter, K., "Evaluation of the Windsor Probe Test for Estimating Compressive Strength of Concrete," Mines Branch

Investigation Report IR 71-50, Ottawa, Canada, 1971.

- [23] Gaynor, R. D., "In-Place Strength of Concrete - A Comparison of Two Test Systems," National Ready-Mix Concrete Association Technical Information Letter No. 272, 1969.
- [24] Watstein, D., "Bond with Reinforcing Steel," ASTM Special Technical Publication No. 169-A, American Society for Testing and Materials, Philadelphia, Pa., 1966.
- [25] Mathey R. G. and Watstein, D., "Investigation of Bond in Beam and Pull-Out Specimens with High-Yield-Strength Deformed Bars," Journal of the American Concrete Institute, Vol. 32, American Concrete Institute, Detroit, Michigan, March, 1961.

Table 1. Distribution of Test Specimens  
to Three Curing Conditions

Type of Specimen	73 °F Cure (22.8 °C)	55 °F Cure (12.8 °C)	35 °F Cure (1.7 °C)
Compressive Test (6 in x 12 in cyl.)	24	30	36
Splitting Tensile Test (6 in x 12 in cyl.)	24	30	36
Pull-out Test (6 in x 8 in cyl.)	24	30	36
NDE Slab (3 ft x 5 ft x 5-1/2 in)	1	1	1

1 inch = 25.40 mm  
1 foot = 304.80 mm

Table 2. Compressive Strength Test Results<sup>a/</sup>

Age	Specimen Number	Cured at 73°F (22.8°C)			Cured at 55°F (12.8°C)			Cured at 35°F (1.7°C)		
		f' <sub>ci</sub>	E <sub>s</sub> @.4f' <sub>ci</sub>	E <sub>s</sub> @.8f' <sub>ci</sub>	f' <sub>ci</sub>	E <sub>s</sub> @.4f' <sub>ci</sub>	E <sub>s</sub> @.8f' <sub>ci</sub>	f' <sub>ci</sub>	E <sub>s</sub> @.4f' <sub>ci</sub>	E <sub>s</sub> @.8f' <sub>ci</sub>
days		psi (MPa)	10 <sup>6</sup> psi (GPa)	10 <sup>6</sup> psi (GPa)	psi (MPa)	10 <sup>6</sup> psi (GPa)	10 <sup>6</sup> psi (GPa)	psi (MPa)	10 <sup>6</sup> psi (GPa)	10 <sup>6</sup> psi (GPa)
1	1	1350	2.06	1.56	1170	1.96	1.36	955	1.78	1.19
	2	1420	2.27	1.61	1180	2.03	1.46	944	1.49	.94
	3	1220	2.64	2.01	1200	1.91	1.36	1040	1.63	.99
	Average	1330 (9.17)	2.32 (16.00)	1.73 (11.93)	1180 (8.14)	1.97 (13.58)	1.39 (9.58)	980 (6.76)	1.63 (11.24)	1.04 (7.17)
	(C.V.,%)	(8)			(1)			(5)		
2	1	1910	2.89	2.32	1470	2.67	1.70	1250	1.67	1.11
	2	1870	3.25	2.50	1520	2.26	1.70	1280	1.83	1.13
	3	2200	2.95	2.20	1450	2.49	1.82	1260	1.67	1.11
	Average	1990 (13.72)	3.03 (20.89)	2.34 (16.13)	1480 (10.20)	2.47 (17.03)	1.74 (12.00)	1260 (8.69)	1.72 (11.86)	1.12 (7.72)
	(C.V.,%)	(9)			(2)			(1)		
3	1	2210	3.51	2.65	1780	2.69	2.04	1400	2.09	1.58
	2	2220	3.61	2.65	1680	2.83	2.17	1340	2.12	1.66
	3	2150	2.72	2.25	1770	2.55	2.00	1420	2.09	1.62
	Average	2190 (15.10)	3.28 (22.61)	2.52 (17.37)	1740 (12.00)	2.69 (18.99)	2.07 (14.27)	1390 (9.58)	2.10 (14.48)	1.62 (11.17)
	(C.V.,%)	(2)			(3)			(3)		
5	1	2460	3.69	2.86	2000	2.99	2.26	1880	2.16	1.56
	2	2480	3.93	2.90	1950	2.89	2.28	1710	2.32	1.70
	3	2710	3.66	2.84	1830	3.40	2.75	1840	2.64	2.08
	Average	2590 (17.86)	3.76 (25.92)	2.87 (19.79)	1930 (13.31)	3.09 (21.30)	2.43 (16.75)	1810 (12.48)	2.37 (16.34)	1.78 (12.27)
	(C.V.,%)	(5)			(4)			(5)		
7	1	2850	3.62	2.78	2510	3.23	2.63	2180	3.29	2.16
	2	2930	3.81	3.05	2640	3.47	3.02	2200	2.55	1.93
	3	2890	3.55	2.78	2550	3.23	2.56	2170	2.80	2.08
	Average	2890 (19.93)	3.66 (25.23)	2.87 (19.79)	2570 (17.72)	3.31 (22.82)	2.74 (18.89)	2180 (15.03)	2.88 (19.86)	2.06 (14.20)
	(C.V.,%)	(1)			(3)			(1)		
14	1	3160	3.59	3.11	2590	3.42	3.03	2700	3.09	2.48
	2	3320	3.71	3.15	2720	3.54	3.02	2810	3.22	2.49
	3	3190	3.65	3.16	2520	3.62	3.03	2640	3.23	2.52
	Average	3230 (22.27)	3.65 (25.17)	3.14 (21.69)	2610 (18.00)	3.53 (24.34)	3.03 (20.89)	2720 (187.54)	3.18 (21.93)	2.50 (17.24)
	(C.V.,%)	(3)			(4)			(3)		
21	1	3210	4.04	3.37	2850	3.68	2.73	2990	3.42	2.62
	2	3270	3.71	3.12	2700	3.40	2.72	3060	3.42	2.74
	3	3500	3.97	3.48	2770	4.16	3.22	3020	3.68	2.87
	Average	3330 (22.96)	3.91 (26.96)	3.32 (22.27)	2770 (19.10)	3.75 (25.86)	2.89 (19.93)	3020 (20.82)	3.51 (24.20)	2.74 (18.89)
	(C.V.,%)	(5)			(3)			(1)		
28	1	3560	4.27	3.54	2790	2.93	3.14	3460	3.73	3.19
	2	3590	4.35	3.54	2810	4.70	3.36	3380	3.99	3.32
	3	3520	4.82	3.91	2950	4.02	3.19	3360	3.39	2.98
	Average	3560 (24.55)	4.48 (30.89)	3.66 (25.23)	2850 (19.65)	3.88 (26.75)	3.23 (22.27)	3400 (23.44)	3.70 (25.51)	3.16 (21.79)
	(C.V.,%)	(1)			(3)			(2)		
42	1	-	-	-	3300	4.04	3.40	3610	4.25	3.62
	2	-	-	-	3420	4.39	3.73	3380	3.81	3.14
	3	-	-	-	3440	4.61	3.73	3250	3.73	3.04
	Average	-	-	-	3390 (23.37)	4.35 (29.99)	3.62 (24.96)	3410 (23.51)	3.93 (27.10)	3.27 (22.55)
	(C.V.,%)				(2)			(5)		

<sup>a/</sup>f' <sub>ci</sub> is the compressive strength at each age. E<sub>s</sub> is the secant modulus of elasticity taken from individual stress-strain curves.  
psi = 1.lbf/in<sup>2</sup> = 6895 pascal C.V. = Coefficient of variation

Table 3. Splitting Tensile Strength Test Results<sup>a/</sup>

Age	Specimen Number	Cured at 73°F (22.8°C)			Cured at 55°F (12.8°C)			Cured at 35°F (1.7°C)		
		f' <sub>sp</sub>	S.D.	C.V.	f' <sub>sp</sub>	S.D.	C.V.	f' <sub>sp</sub>	S.D.	C.V.
days		psi (kPa)	psi (kPa)	%	psi (kPa)	psi (kPa)	%	psi (kPa)	psi (kPa)	%
1	1	207			164			93		
	2	201			142			116		
	3	191			148			129		
	Average	200 (1380)	8 (55)	4	151 (1041)	11 (76)	8	113 (779)	18 (124)	16
2	1	282			209			138		
	2	241			214			166		
	3	231			207			156		
	Average	251 (1730)	27 (186)	11	210 (1448)	4 (28)	2	153 (1054)	14 (97)	9
3	1	297			202			163		
	2	303			227			195		
	3	275			223			199		
	Average	292 (2013)	15 (103)	5	217 (1496)	13 (90)	6	189 (1282)	20 (138)	11
5	1	331			288			218		
	2	313			246			268		
	3	293			238			245		
	Average	312 (2151)	19 (131)	6	257 (1772)	27 (186)	10	244 (1682)	25 (172)	10
7	1	331			286			254		
	2	305			290			251		
	3	350			320			316		
	Average	329 (2268)	23 (158)	7	299 (2062)	19 (131)	6	273 (1882)	37 (255)	13
14	1	434			286			326		
	2	365			329			317		
	3	359			355			350		
	Average	386 (2661)	42 (290)	11	323 (2227)	35 (241)	11	331 (2282)	17 (117)	5
21	1	426			387			384		
	2	436			395			355		
	3	357			365			350		
	Average	406 (2799)	43 (296)	11	382 (2634)	16 (110)	4	363 (2503)	18 (124)	5
28	1	469			357			376		
	2	450			400			345		
	3	381			374			385		
	Average	434 (2992)	47 (324)	11	377 (2599)	22 (152)	6	368 (2537)	21 (145)	6
42	1	-			430			357		
	2	-			407			384		
	3	-			396			372		
	Average	-			411 (2834)	17 (117)	4	371 (2558)	13 (90)	4

<sup>a/</sup> Splitting Tensile Strength ( $f'_{sp}$ ) =  $\frac{2P}{\pi DL}$ ; Where P = load at splitting, D = diameter of specimen (6 in = 15 cm) and L = length of specimen (12 in = 30 cm), psi = 1 lbf/in<sup>2</sup> = 6895 pascal. S.D. = Standard deviation and C.V. = Coefficient of variation.

Table 4. Pull-Out Bond Strength Test Results<sup>a/</sup>

Age	Specimen Number	Cured at 73°F (22.8°C)			Cured at 55°F (12.8°C)			Cured at 35°F (1.7°C)		
		P Maximum	P @ Slip of .001 in	P @ Slip of .002 in	P Maximum	P @ Slip of .001 in	P @ Slip of .002 in	P Maximum	P @ Slip of .001 in	P @ Slip of .002 in
days		Kip (kN)	Kip (kN)	Kip (kN)	Kip (kN)	Kip (kN)	Kip (kN)	Kip (kN)	Kip (kN)	Kip (kN)
1	1	15.00	7.1	8.5	10.50	5.3	6.3	8.53	3.7	4.5
	2	14.15	4.6	6.5	11.30	4.9	5.9	8.43	4.8	5.7
	3	14.60	6.3	8.5	12.05	6.1	7.6	9.58	3.9	4.9
	Average (C.V.,%)	14.58 (64.85) (3)	6.0 (26.69)	7.8 (34.69)	11.28 (50.17)	5.4 (24.02)	6.6 (29.36)	8.85 (39.36) (2)	4.1 (18.24)	5.0 (22.24)
2	1	19.20	8.9	10.6	13.45	6.2	7.3	12.45	5.5	6.7
	2	15.65	6.5	8.4	14.10	7.6	8.9	12.85	6.0	7.0
	3	18.20	7.0	8.9	13.90	7.6	8.6	12.30	-	-
	Average (C.V.,%)	17.68 (78.64) (10)	7.5 (33.36)	9.3 (41.37)	13.82 (61.47) (2)	7.1 (31.58)	8.3 (36.92)	12.53 (55.73) (2)	5.8 (25.80)	6.9 (30.69)
3	1	19.15	7.8	10.0	17.35	9.2	10.8	13.80	7.9	9.1
	2	20.70	9.2	11.5	16.65	11.1	12.0	14.55	8.5	10.1
	3	20.50	8.7	11.0	17.35	9.6	11.2	14.05	7.9	9.1
	Average (C.V.,%)	20.12 (89.49) (4)	8.6 (38.25)	10.8 (48.04)	17.12 (76.15) (2)	10.0 (44.48)	11.3 (50.26)	14.13 (62.85) (2)	8.1 (36.03)	9.4 (41.81)
5	1	20.05	11.0	12.6	20.25	10.0	11.7	17.05	10.9	13.5
	2	23.50	10.2	13.3	18.90	10.5	12.2	18.70	12.1	13.5
	3	21.25	10.8	13.8	19.95	-	-	17.85	10.1	11.8
	Average (C.V.,%)	21.60 (96.08) (8)	10.7 (47.59)	13.2 (58.71)	19.70 (87.63) (4)	10.3 (45.81)	12.0 (53.38)	17.87 (79.49) (5)	11.0 (48.93)	12.9 (57.38)
7	1	23.85	11.2	13.5	22.55	11.2	13.1	19.80	11.1	13.3
	2	23.90	10.6	13.0	18.55	12.5	14.2	19.90	11.5	13.3
	3	23.35	9.0	11.6	22.65	12.0	13.7	20.40	13.0	14.5
	Average (C.V.,%)	23.70 (105.42) (1)	10.3 (45.81)	12.7 (56.49)	21.25 (94.52) (11)	11.9 (52.93)	13.7 (60.94)	20.03 (89.09) (2)	11.9 (52.93)	13.7 (60.94)
14	1	26.15	11.8	14.5	23.00	13.4	15.4	22.60	13.2	16.4
	2	26.40	15.4	18.0	24.45	13.8	15.7	23.45	12.5	15.5
	3	25.23	8.0	10.9	25.10	14.8	16.5	22.15	-	-
	Average (C.V.,%)	25.93 (115.34) (2)	11.7 (52.04)	14.5 (64.50)	24.18 (107.55) (4)	14.0 (62.27)	15.9 (70.72)	22.73 (101.10) (3)	12.9 (57.38)	16.0 (71.17)
21	1	27.10	16.2	20.7	26.00	14.8	17.0	25.65	17.6	20.2
	2	24.85	12.2	14.7	25.85	14.9	17.2	25.55	15.2	18.0
	3	25.70	-	-	26.10	14.7	16.8	25.80	16.1	18.5
	Average (C.V.,%)	25.88 (115.11) (4)	14.2 (63.16)	17.7 (78.73)	25.98 (115.56) (1)	14.8 (65.83)	17.0 (75.62)	25.67 (114.18) (1)	16.3 (72.50)	18.9 (84.07)
28	1	28.05	14.8	17.7	27.15	16.8	18.7	26.50	15.8	17.9
	2	26.35	15.0	17.8	24.60	13.6	16.0	26.80	17.0	19.5
	3	27.25	11.3	15.1	27.20	14.7	17.5	25.10	14.8	17.5
	Average (C.V.,%)	27.22 (121.07) (3)	13.7 (60.94)	16.9 (75.17)	26.32 (117.07) (6)	15.0 (66.72)	17.4 (77.40)	26.13 (116.23) (3)	15.9 (70.72)	18.3 (81.40)
42	1	-	-	-	26.15	17.6	19.8	28.60	19.7	23.0
	2	-	-	-	27.25	17.2	19.3	26.10	18.8	21.7
	3	-	-	-	26.00	17.3	19.2	29.10	19.0	21.9
	Average (C.V.,%)	-	-	-	26.46 (117.69) (3)	17.4 (77.40)	19.4 (81.84)	27.93 (124.23) (7)	19.2 (85.40)	22.2 (98.75)

<sup>a/</sup>P is the maximum pull-out load. Slip is the movement of the unloaded end of the No. 6 bar relative to the surface of the concrete. Kip = 1000 lbf. = 4448 N. Slip of .001 in = .0254 mm. C.V. = Coefficient of variation.

Table 5. Impact Penetration Test Results <sup>a/</sup>

Age days	Cured at 73 °F (22.8 °C)				Cured at 55 °F (12.8 °C)				Cured at 35 °F (1.7 °C)			
	Number of Probes <sup>b/</sup>	Probe Measurements (P)		C.V. <sup>d/</sup> %	Number of Probes <sup>b/</sup>	Probe Measurements (P)		C.V. <sup>d/</sup> %	Number of Probes <sup>b/</sup>	Probe Measurements (P)		C.V. <sup>d/</sup> %
		Average P in (cm)	S.D. <sup>c/</sup> in (mm)			Average P in (cm)	S.D. <sup>c/</sup> in (mm)			Average P in (cm)	S.D. <sup>c/</sup> in (mm)	
1	3L	1.825L(4.64)	--	--	3L	1.675L(4.25)	--	--	3L	1.550L(3.94)	--	--
2	6L	2.075L(5.27)	--	--	3L	1.925L(4.89)	--	--	3L	1.750L(4.45)	--	--
3	6L	2.079L(5.28)	0.107(2.7)	5.1	6L	1.918L(4.87)	0.097(2.5)	5.0	6L	1.910L(4.85)	0.188(4.8)	9.8
4	6	1.453(3.69)	0.179(4.6)	12.3	5L	2.137L(5.52)	0.071(1.8)	8.0	6	1.283(3.26)	0.133(3.4)	10.4
7	6	1.540(3.91)	0.108(2.7)	7.0	6	1.533(3.89)	0.142(3.6)	9.3	6	1.518(3.86)	0.208(5.3)	13.7
14	6	1.739(4.42)	0.150(3.8)	8.7	6	1.583(3.91)	0.145(3.7)	9.2	6	1.583(4.02)	0.168(4.3)	10.6
28	6	1.755(4.46)	0.141(3.6)	8.1	6	1.698(4.31)	0.129(3.3)	7.6	6	1.742(4.42)	0.045(1.1)	2.6

a/ Probe measurement is the length of the probe above the surface of the concrete. When the number of probes was 3 the measurement was obtained with an averaging device furnished by the probe manufacturer. All other measurements were made on the individual probes with a steel rule.

b/ The letter "L" beside the number of probes and the average P indicates that the low-power setting was used when driving the probes. The standard power setting was used for all others.

c/ S.D. is the standard deviation.

d/ C.V. is the coefficient of variation.



Table 6. Rebound Hammer Test Results<sup>a/</sup>

Age days	Cured at 73°F (22.8°C)				Cured at 55°F (12.8°C)				Cured at 35°F (1.7°C)			
	Number of tests	Rebound Readings (R)		Number of tests	Rebound Readings (R)		Number of tests	Rebound Readings (R)		Number of tests	Rebound Readings (R)	
		Average R	S.D. <sup>b/</sup>		C.V. <sup>c/</sup>	Average R		S.D.	C.V.		Average R	S.D.
1	11	11.2	0.9	8.2	<10	---	5	<10	---	3	<10	---
2	15	13.3	1.2	10.0	<10	---	8	<10	---	14	12.0	1.0
3	15	13.5	1.5	12.1	12.2	1.7	13	12.2	1.7	14	12.4	1.7
5	15	14.5	1.2	7.6	12.1	1.8	14	12.1	1.8	15	15.7	2.3
7	15	17.1	0.7	4.4	14.1	1.9	15	14.1	1.9	15	15.9	1.6
14	15	19.2	2.9	18.0	15.5	2.3	15	15.5	2.3	15	16.1	1.0
21	15	18.7	2.3	12.4	18.6	3.2	15	18.6	3.2	15	18.6	2.4
28	15	18.7	2.3	11.8	15.2	3.2	15	15.2	3.2	15	19.5	2.2

<sup>a/</sup> Minimum measurement with instrument was 10 units. Number of tests indicated are those with a reading of 10 or higher. Total number of measurements made for each set was 15.

<sup>b/</sup> S.D. is the standard deviation.

<sup>c/</sup> C.V. is the coefficient of variation.

Table 7. Mean Temperature of Concrete During Each Age Interval

Age Interval days	Mean Temperature During Interval					
	73 °F (22.8 °C)		55 °F (12.8 °C)		35 °F (1.7 °C)	
	°F	(°C)	°F	(°C)	°F	(°C)
0-1	79.9	(26.6)	58.8	(14.9)	55.9	(13.3)
1-2	72.8	(22.7)	58.4	(14.7)	38.6	(3.7)
2-3	73.0	(22.8)	58.3	(14.6)	38.1	(3.4)
3-5	73.0	(22.8)	57.5	(14.2)	36.7	(2.6)
5-7	72.5	(22.5)	57.2	(14.0)	35.9	(1.9)
7-14	72.3	(22.4)	56.5	(13.6)	38.4	(3.6)
14-21	73.4	(23.0)	56.4	(13.6)	41.9	(5.9)
21-28	72.8	(22.7)	56.4	(13.6)	42.0	(5.6)
28-42	---		55.1	(12.8)	35.5	(1.9)

Table 8. Maturity Value of Concrete

Age Interval (days)	Maturity (M), °F-day (°C-day)					
	73 °F (22.8 °C)		55 °F (12.8 °C)		35 °F (1.7 °C)	
0-1	69.9	(38.8)	48.8	(27.1)	45.9	(25.5)
0-2	132.7	(73.7)	97.2	(54.0)	74.5	(41.4)
0-3	195.7	(108.7)	145.5	(80.8)	102.6	(57.0)
0-5	321.7	(178.7)	240.5	(133.6)	156.1	(86.7)
0-7	446.7	(248.2)	334.8	(186.0)	207.9	(115.5)
0-14	882.9	(490.5)	660.3	(366.8)	407.0	(226.1)
0-21	1326.4	(736.9)	985.1	(547.3)	630.1	(350.1)
0-28	1764.8	(980.4)	1309.6	(727.6)	854.3	(474.6)
0-42	---		1941.6	(1078.7)	1212.1	(673.4)

Table 9. Statistical Properties Associated with the Regression Equations

Type of Test	Temp °F °C	a	b	S <sub>a</sub>	S <sub>b</sub>	S
Compressive Strength $f'_{ci} = a + b \log M$	73 22.8	-1311.60	1524.35	244.03	92.70	121.44
	55 12.8	-1060.73	1309.35	275.23	105.75	162.91
	35 1.7	-2227.71	1872.32	187.20	76.96	108.21
	all data	-1504.44	1548.33	219.12	85.78	214.82
Elastic Modulus $E_{Si} = a + b \log M$	73 22.8	0.39	1.21	0.53	0.20	0.26
	55 12.8	-0.27	1.37	0.17	0.06	0.10
	35 1.7	-1.30	1.71	0.19	0.08	0.11
	all data	-0.58	1.49	0.26	0.10	0.26
Splitting Tensile Strength $f'_{spi} = a + b \log M$	73 22.8	-89.65	160.48	14.68	9.58	7.31
	55 12.8	-123.82	162.93	19.73	7.58	11.68
	35 1.7	-199.40	195.36	34.06	14.00	19.69
	all data	-145.32	175.18	19.93	7.80	19.54
Pull Out Strength $P_i = a + b \log M$	73 21.8	-4.29	10.40	1.26	0.52	0.46
	55 12.8	-0.31	11.56	1.13	0.47	0.53
	35 1.7	-14.98	14.66	1.58	0.71	0.70
	all data	-9.76	12.37	1.35	0.57	1.02

S<sub>a</sub> : Standard error of the regression coefficient a

S<sub>b</sub> : Standard error of the regression coefficient b

S : Sample standard deviation from regression line  
(Residual standard deviation)

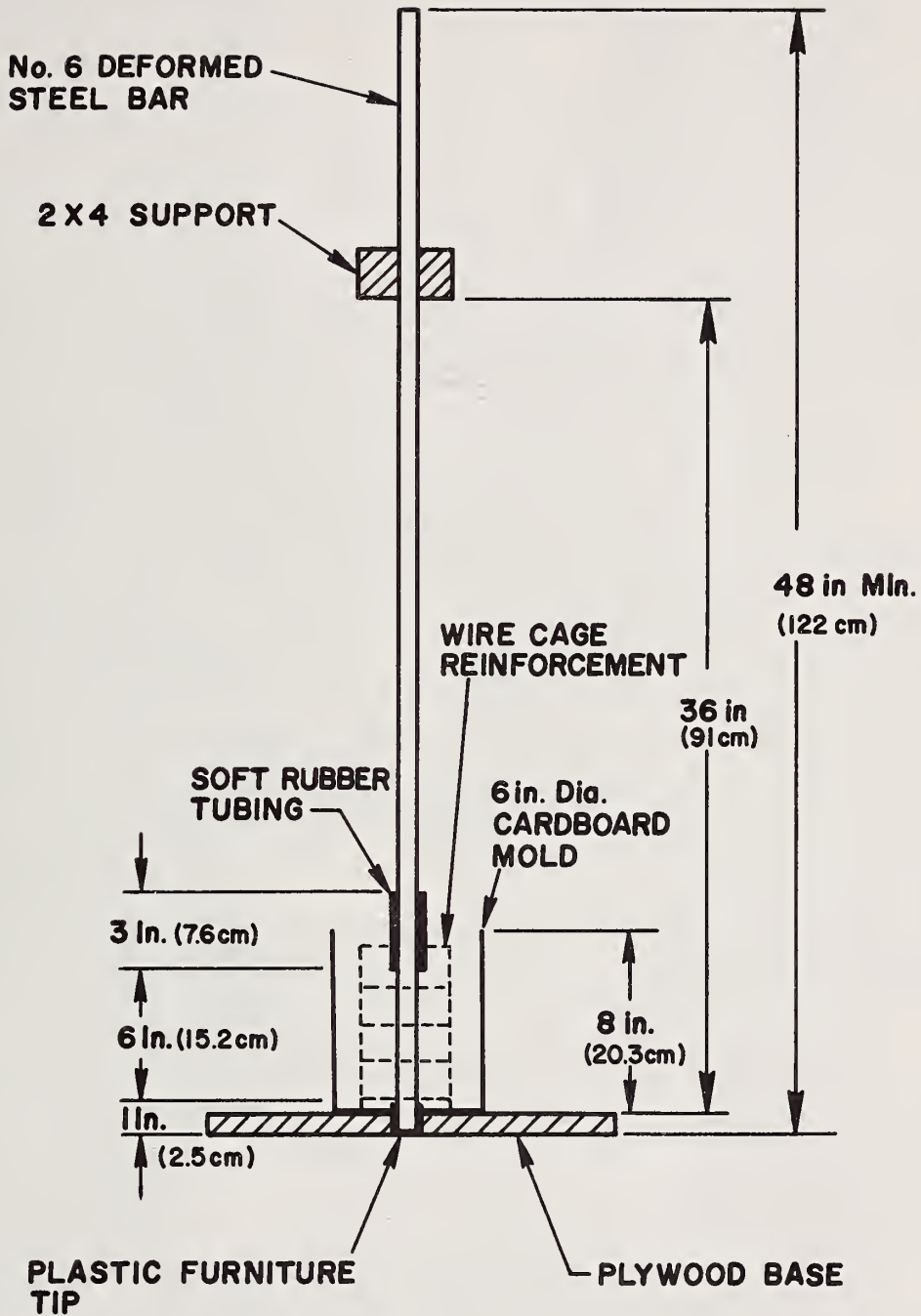


FIGURE 1 Section Through Pull-out Specimen Rack and Mold

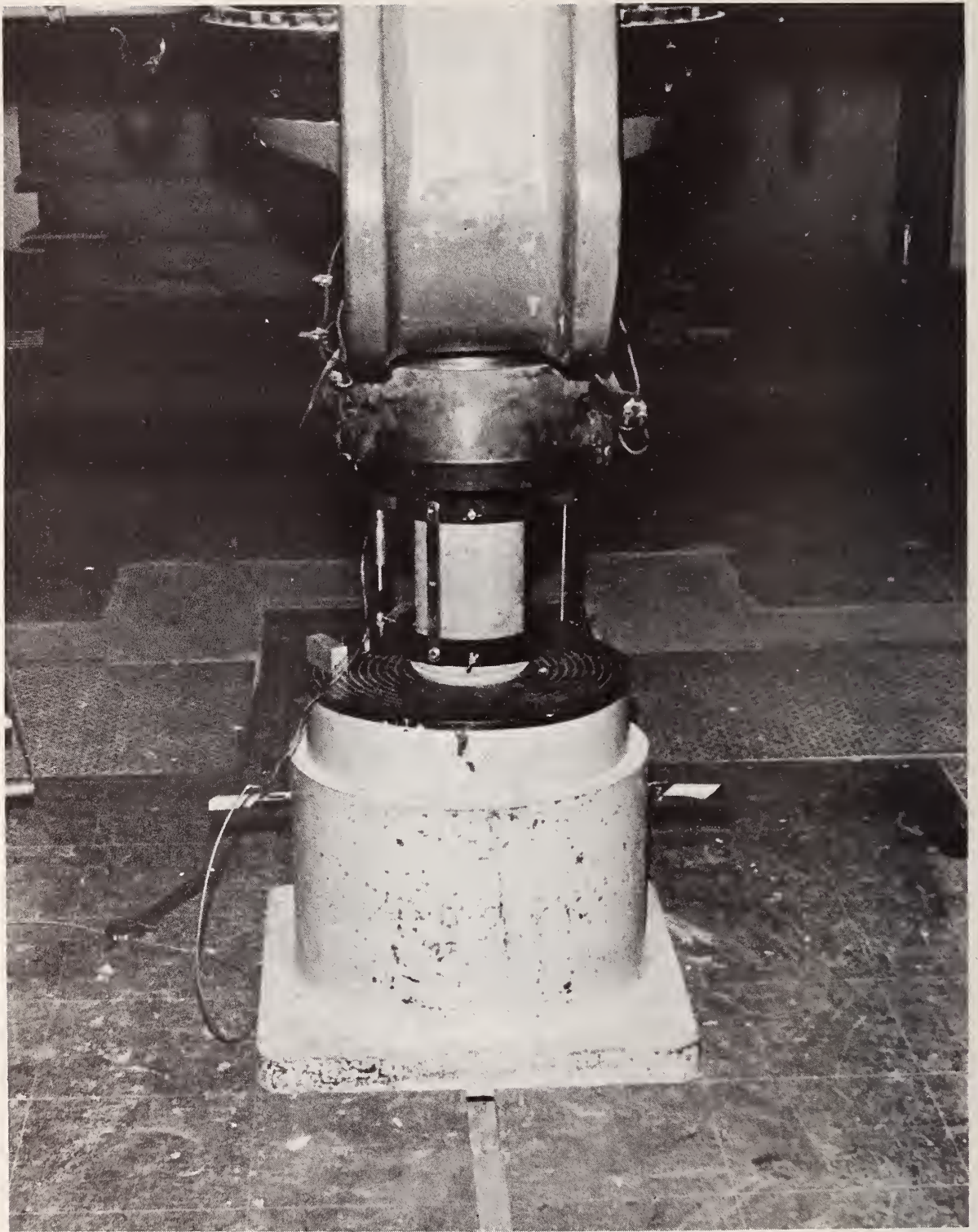


FIGURE 2 Compressive Test of Cylinder

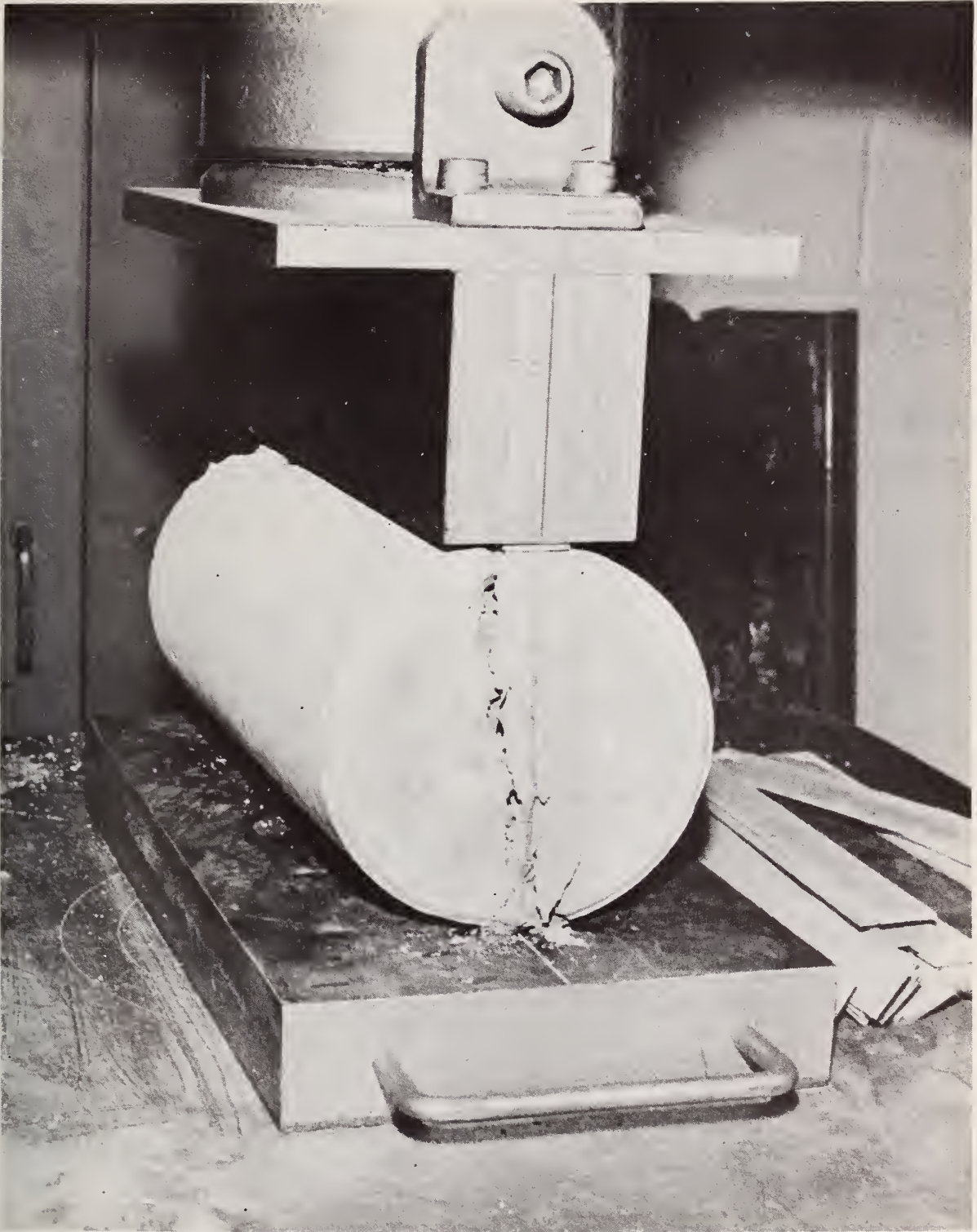


FIGURE 3 Splitting Tensile Test of Cylinder

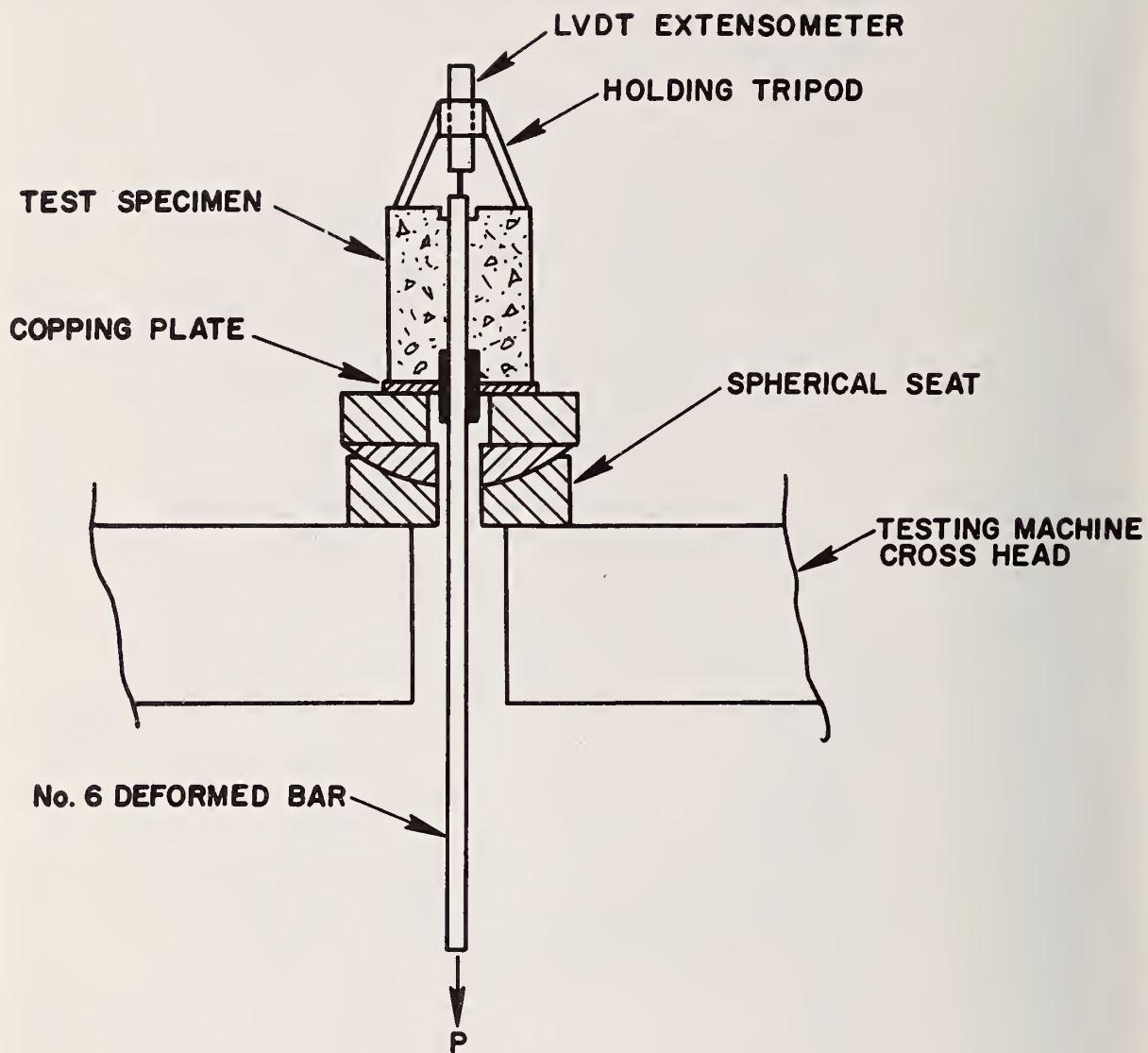


FIGURE 4 Pull-out Test Setup



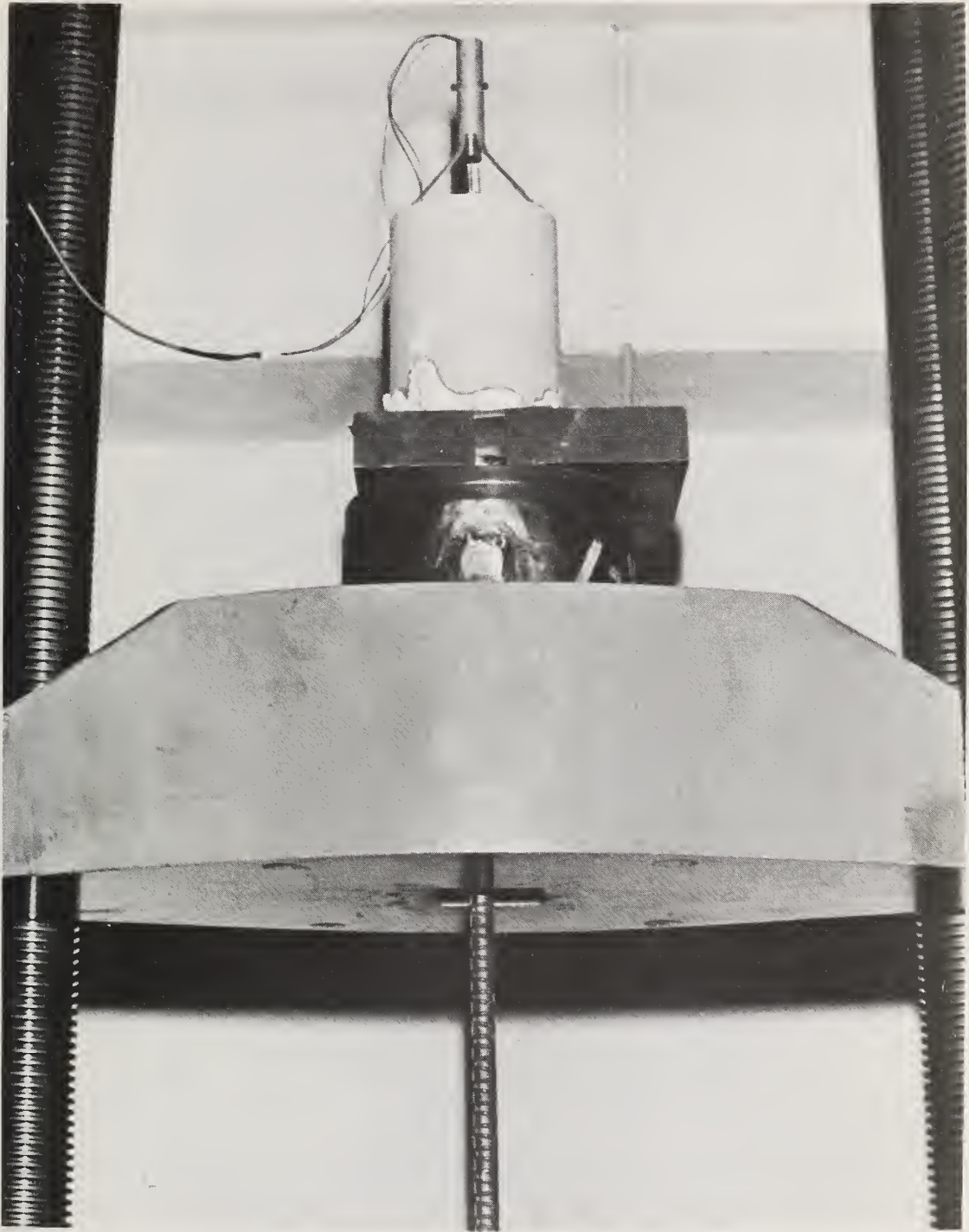


FIGURE 5 Pull-out Bond Test



FIGURE 6 Probe Penetration Test



FIGURE 7 A Device Used to Measure the Average Penetration of Three Probes



FIGURE 8 Rebound Hammer Test

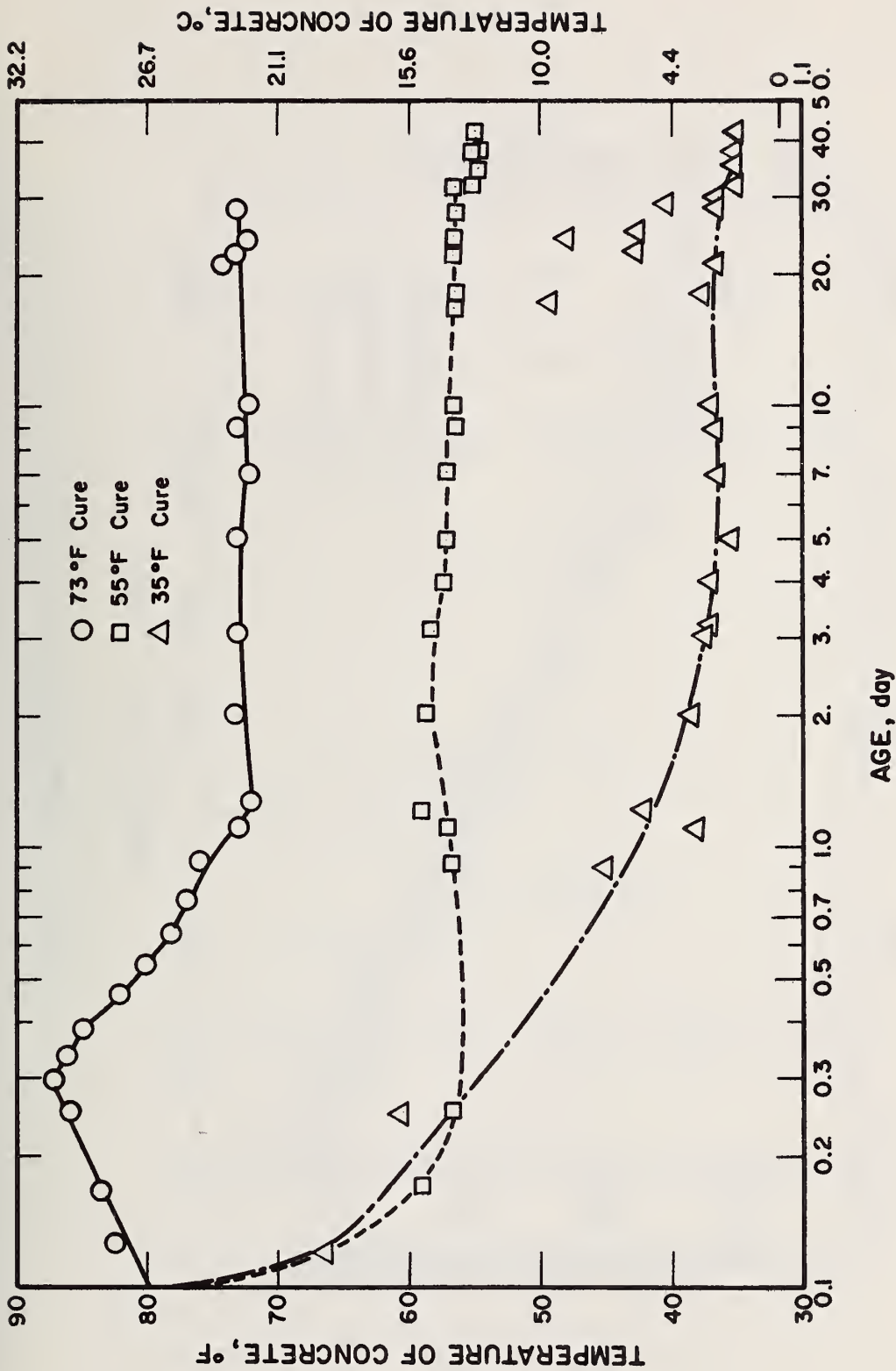


FIGURE 9 Cylinder Temperatures during Curing Period

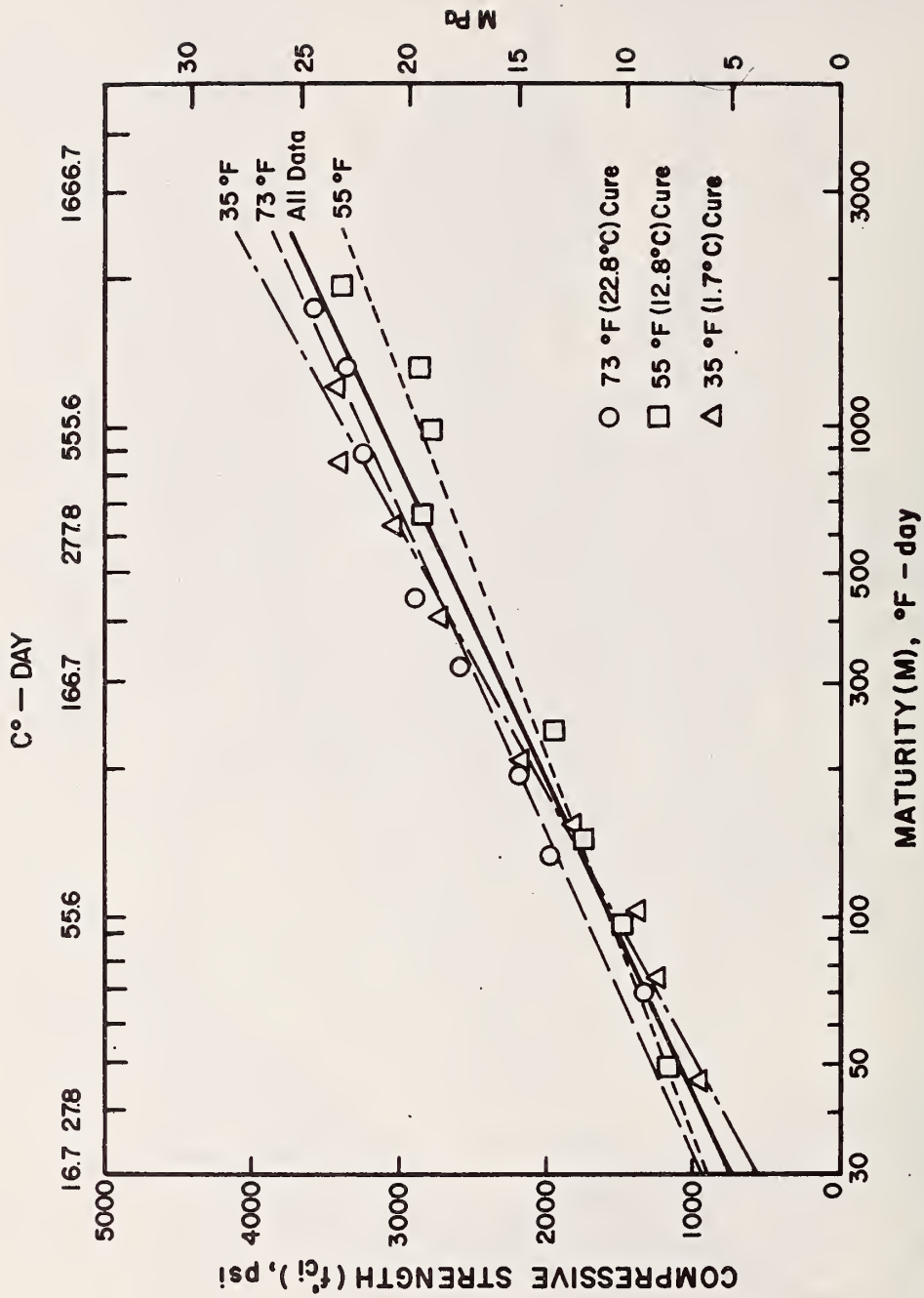


FIGURE 10 Compressive Strength vs. Maturity

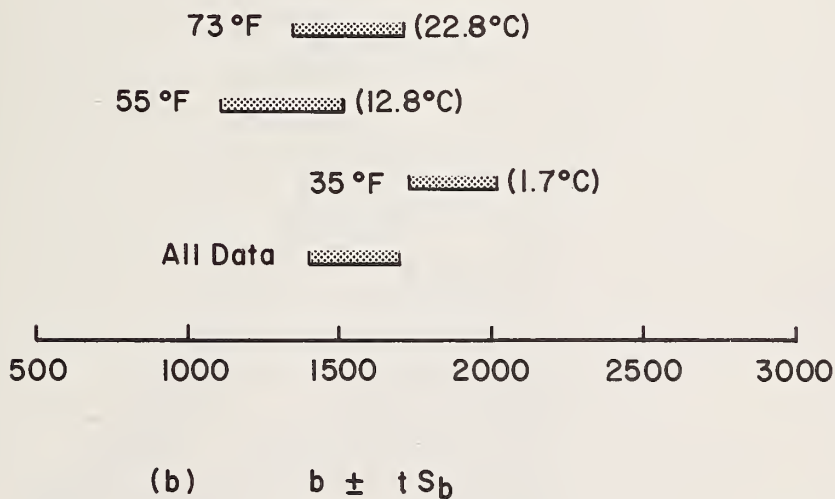
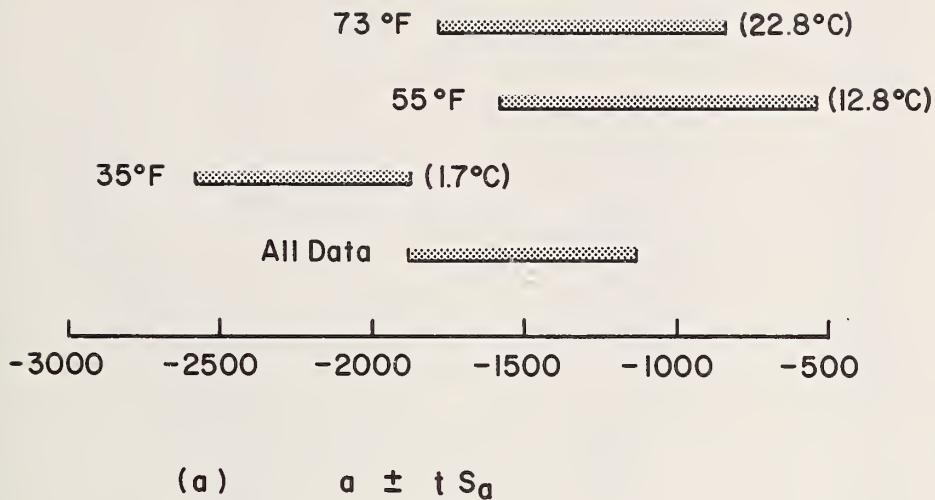


FIGURE 11 The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Compressive Strength vs. Maturity

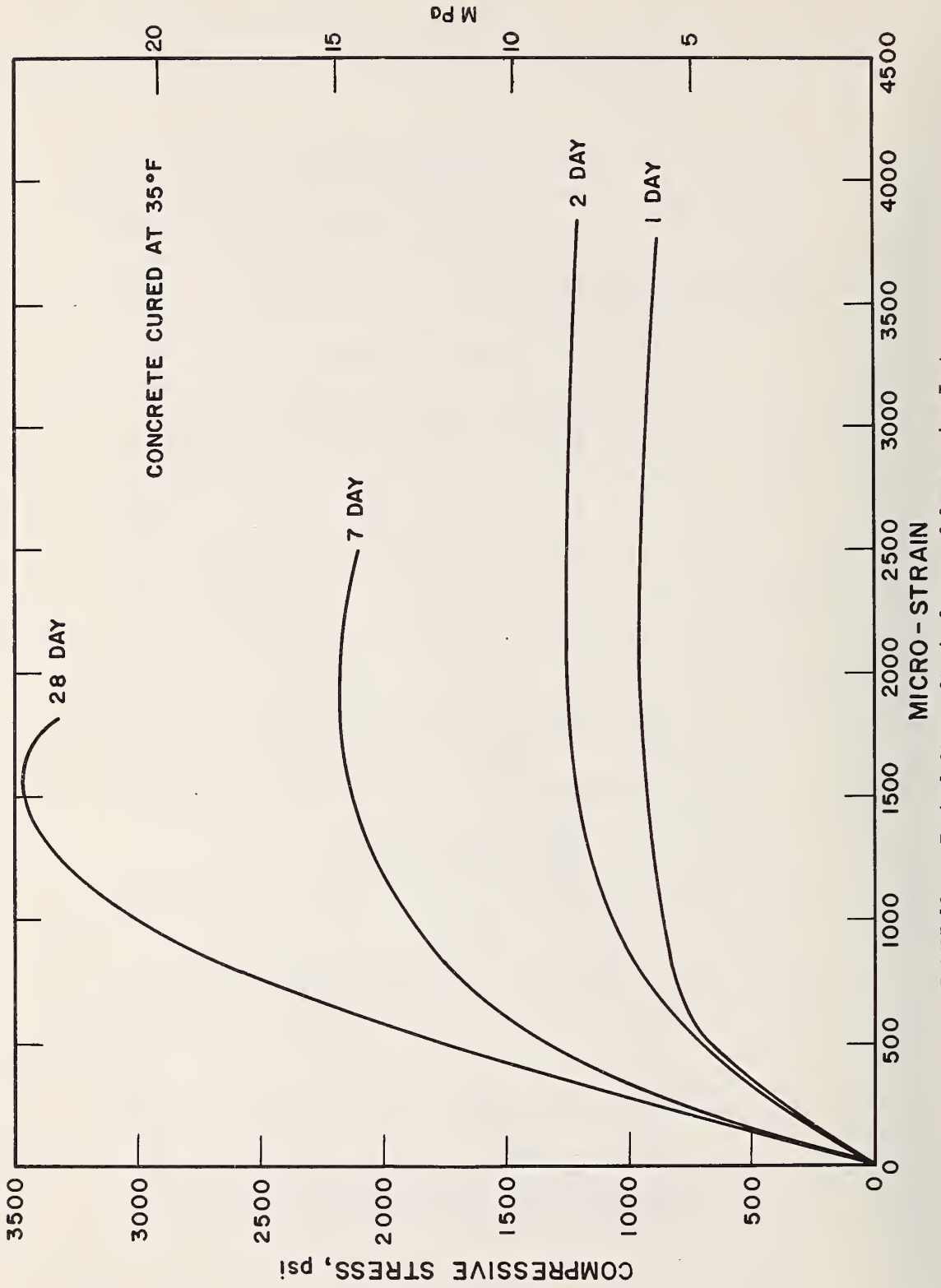


FIGURE 12 Typical Stress-Strain Curves of Compressive Tests of Cylinders cured at 35°F (1.7 °C)



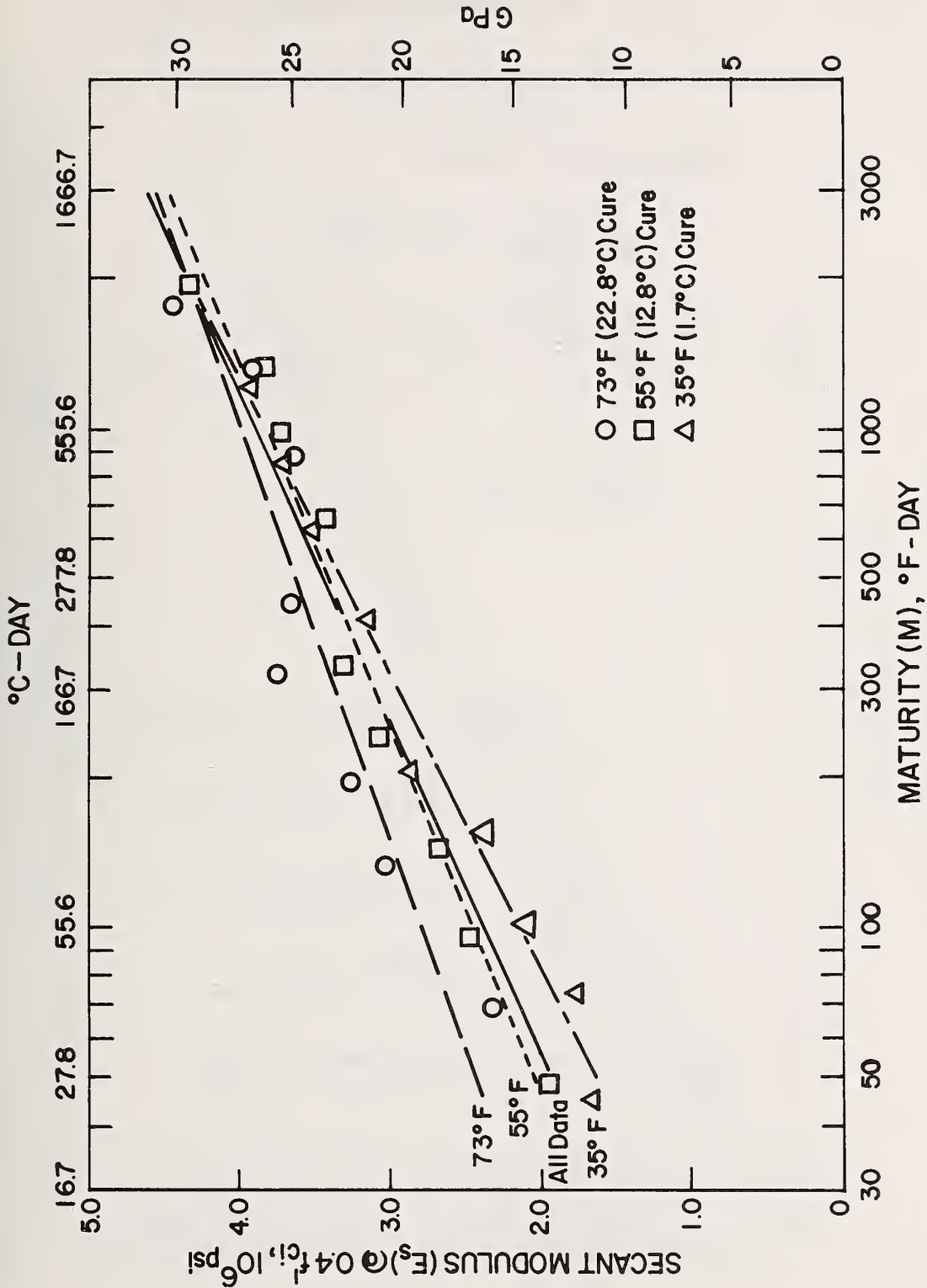


FIGURE 13 Secant Modulus vs. Maturity

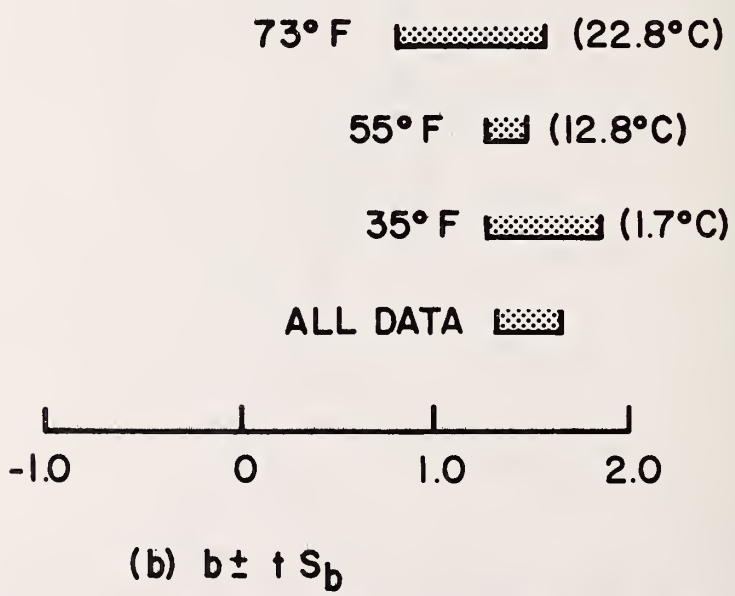
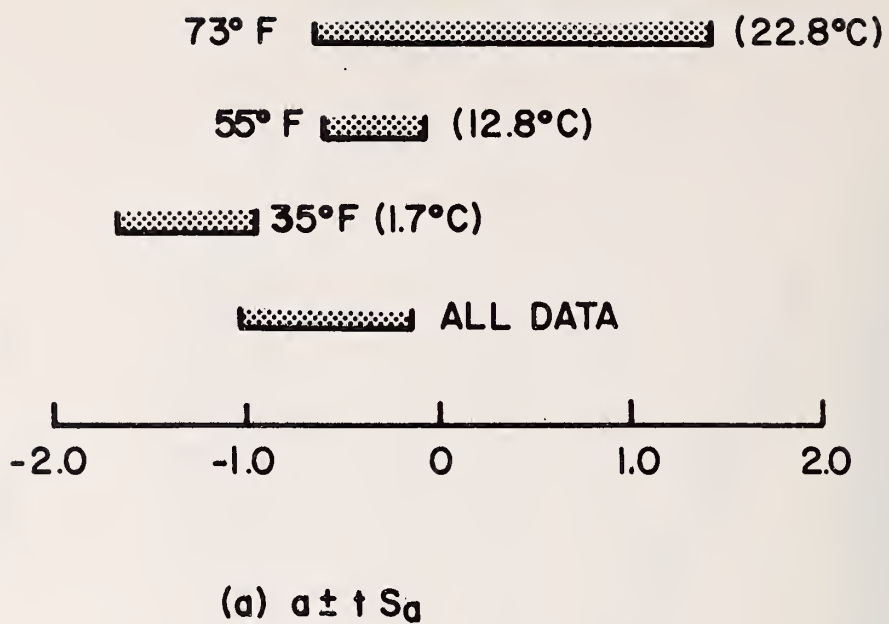


FIGURE 14 The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Secant Modulus vs. Maturity

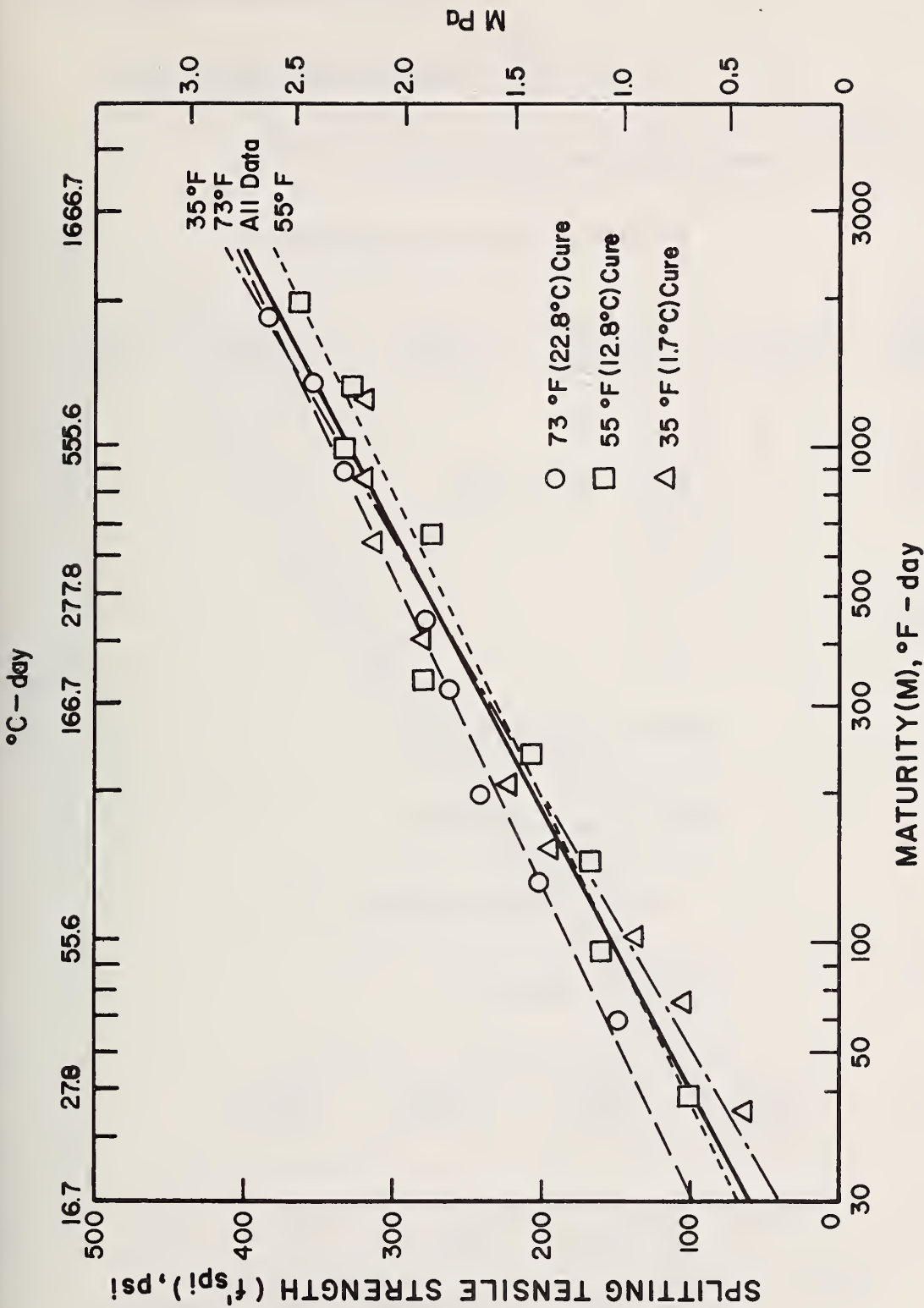
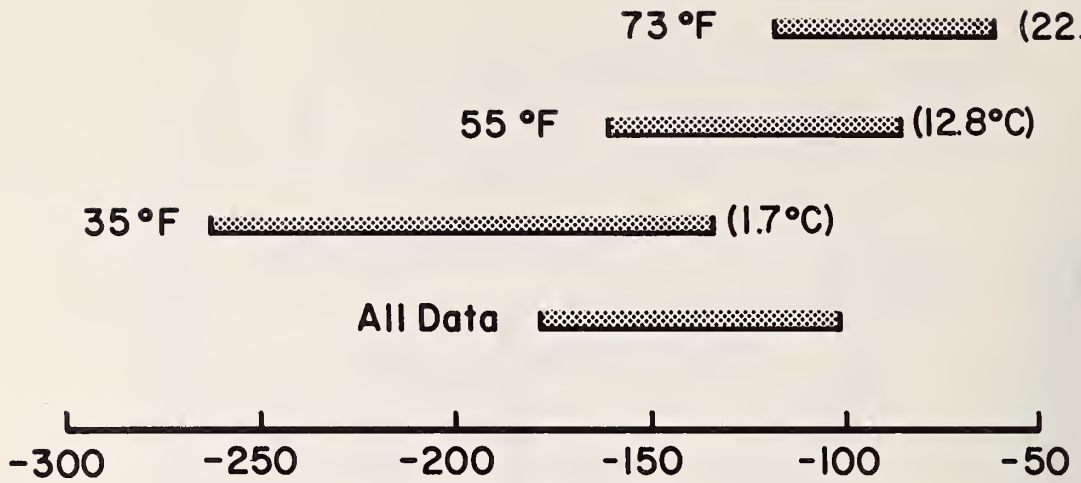
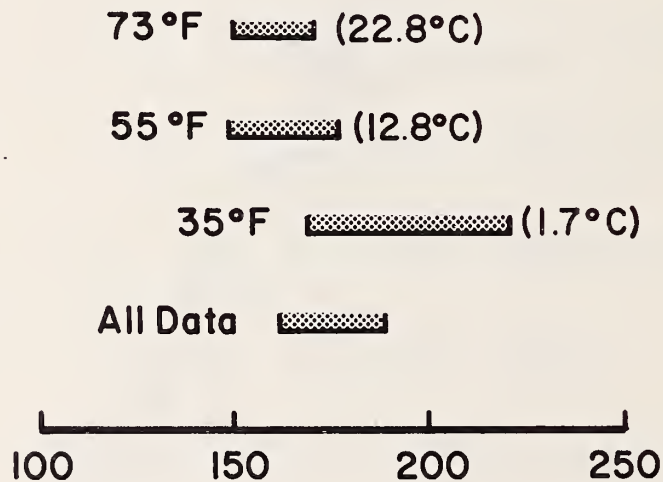


FIGURE 15 Splitting Tensile Strength vs. Maturity



(a)  $a \pm t S_a$



(b)  $b \pm t S_b$

FIGURE 16 The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Splitting Tensile Strength vs. Maturity

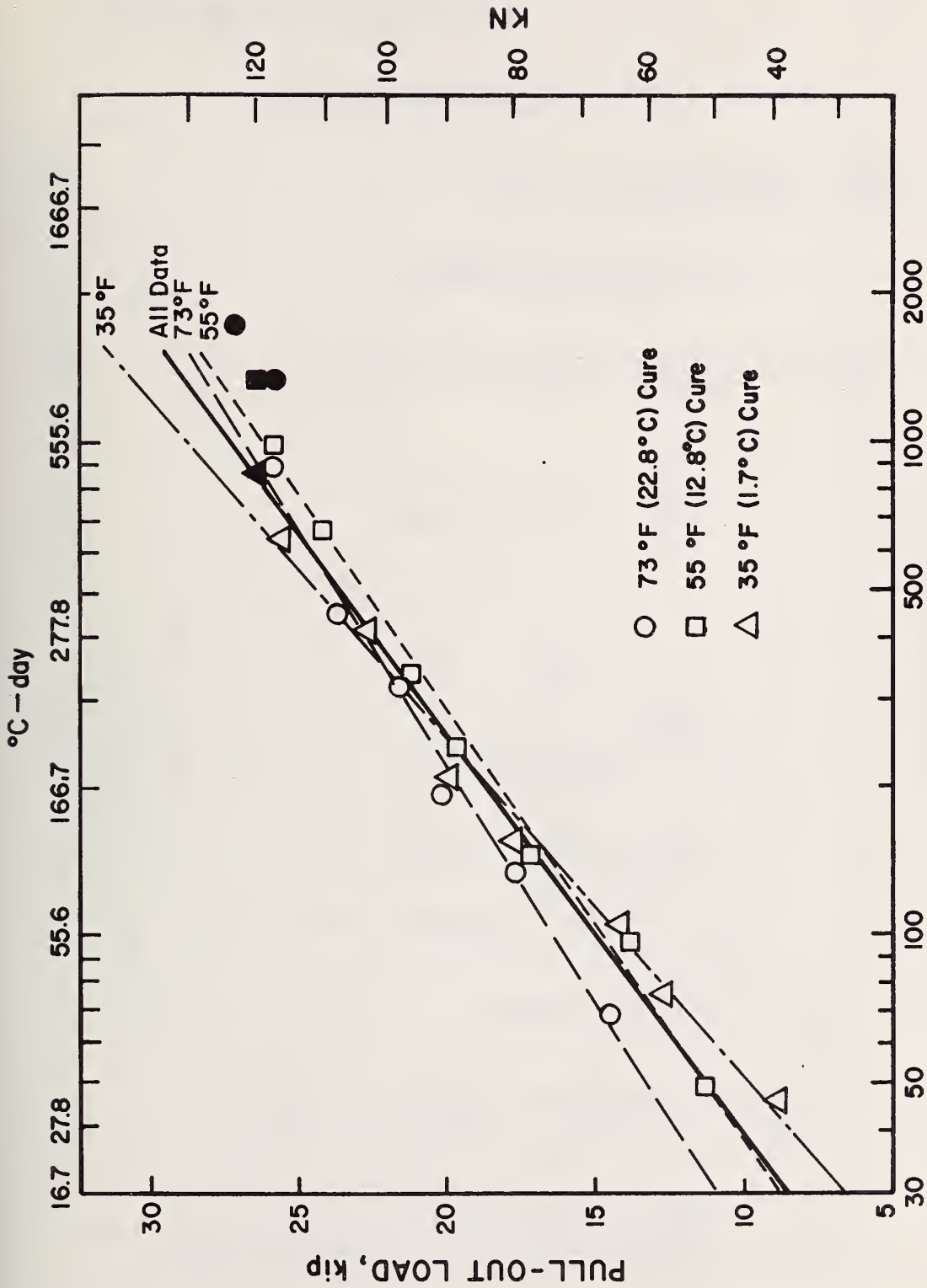
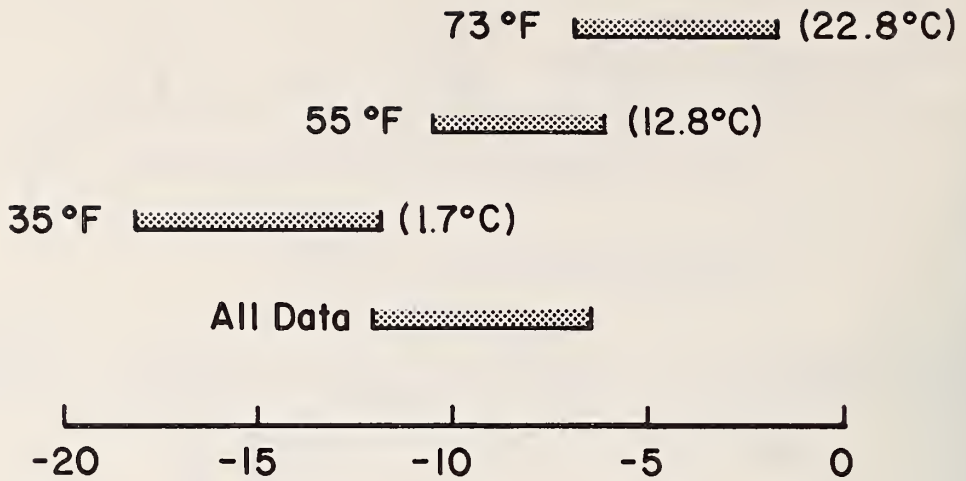
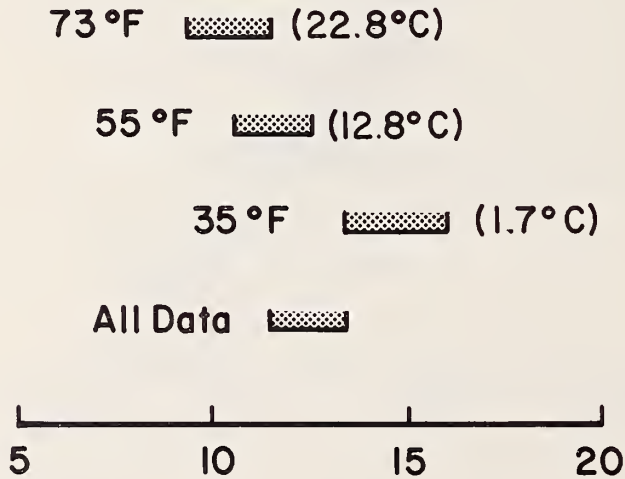


FIGURE 17 Pull-out Load vs. Maturity



(a)  $a \pm t S_a$



(b)  $b \pm t S_b$

FIGURE 18 The Lower and Upper Limits of Intercepts and Slopes of Regression Lines of Pull-out Loads vs. Maturity

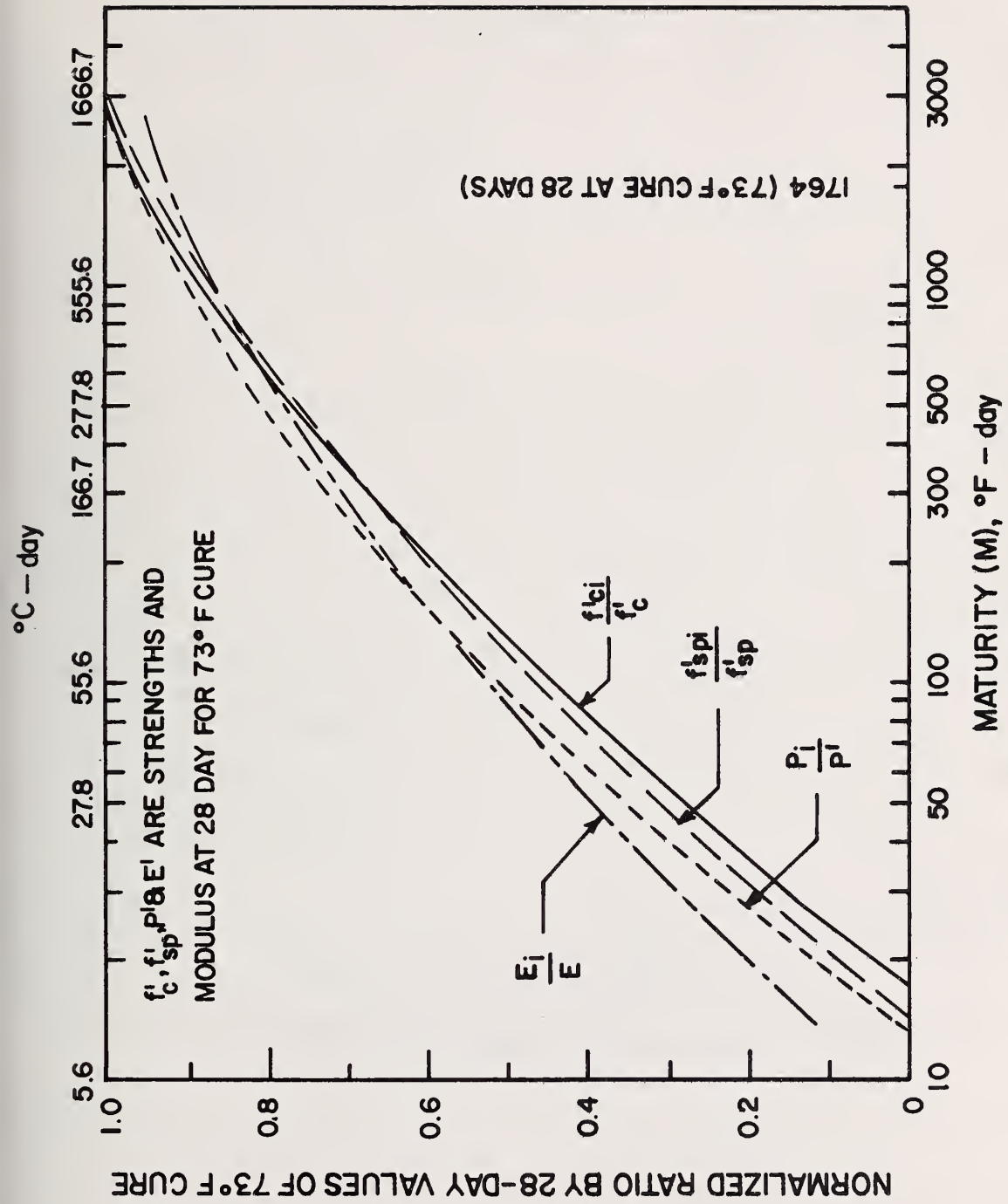


FIGURE 19 Normalized Mechanical Properties With Respect To 28-day Values vs. Maturity

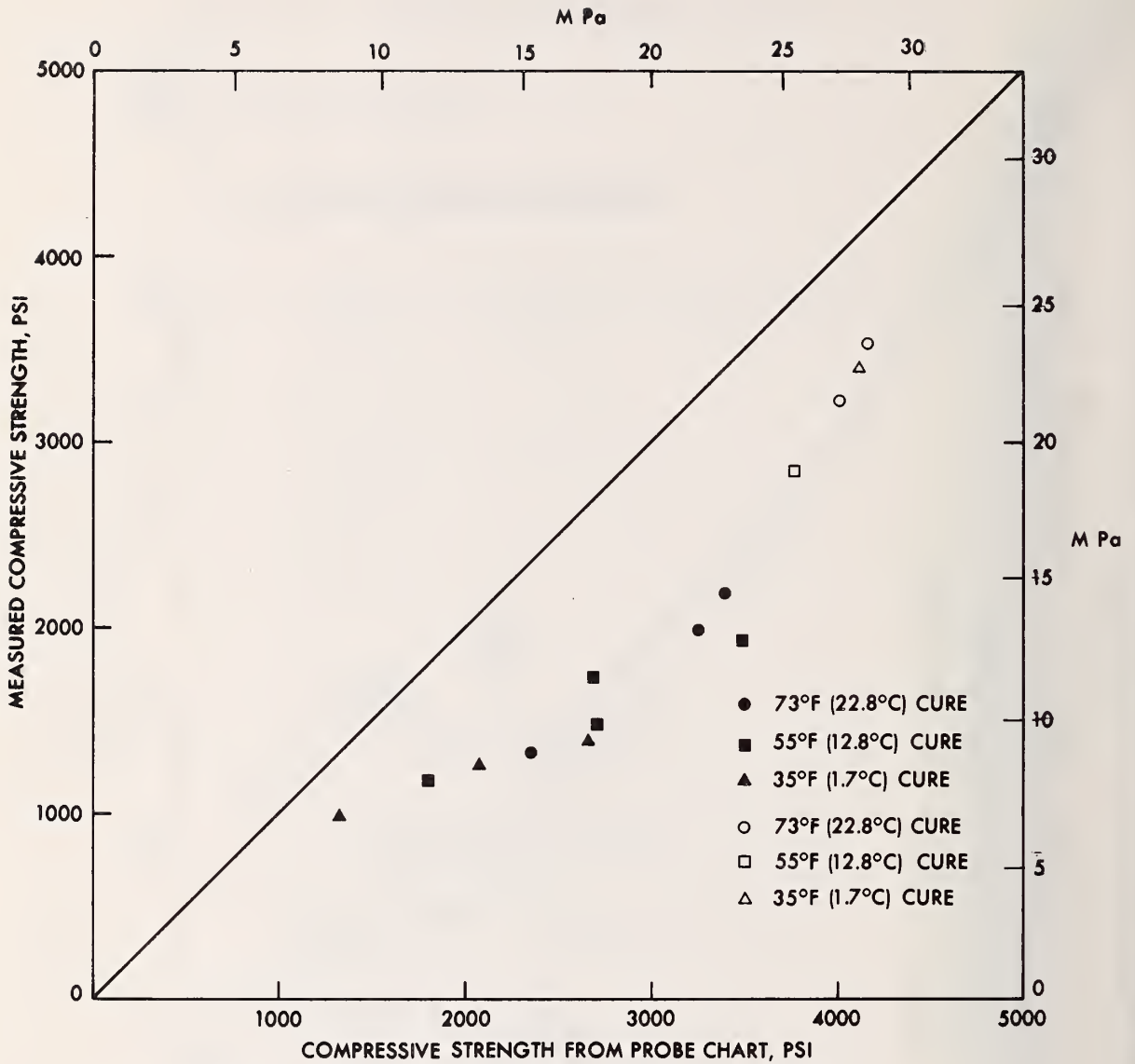


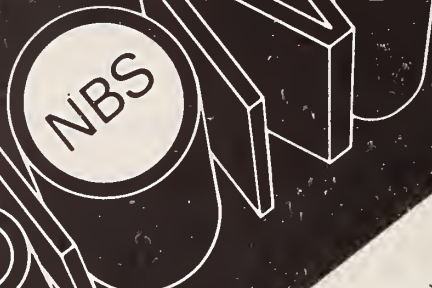
FIGURE 20 Comparison of Measured Compressive Strength vs. Compressive Strength from Probe Chart



U.S. DEPT. OF COMM. BIBLIOGRAPHIC DATA SHEET	1. PUBLICATION OR REPORT NO. Technical Note 932	2. Gov't Accession No.	3. Recipient's Accession No.
4. TITLE AND SUBTITLE  CONCRETE STRENGTH DURING CONSTRUCTION		5. Publication Date December 1976	
		6. Performing Organization Code	
7. AUTHOR(S) H. S. Lew, T. W. Reichard and J. R. Clifton		8. Performing Organ. Report No.	
9. PERFORMING ORGANIZATION NAME AND ADDRESS  NATIONAL BUREAU OF STANDARDS DEPARTMENT OF COMMERCE WASHINGTON, D.C. 20234		10. Project/Task/Work Unit No.	
		11. Contract/Grant No.	
12. Sponsoring Organization Name and Complete Address (Street, City, State, ZIP)  Same as No. 9		13. Type of Report & Period Covered Interim	
		14. Sponsoring Agency Code	
15. SUPPLEMENTARY NOTES The content of this report will be published as an ACI Symposium paper in mid-1977 under the title of "Mechanical Properties of Concrete at Early Ages."			
16. ABSTRACT (A 200-word or less factual summary of most significant information. If document includes a significant bibliography or literature survey, mention it here.) <p>The early strength gain characteristics of a concrete at various temperatures was investigated in this study. In addition, the applicability of two widely known non-destructive evaluation methods were examined for the purpose of determining the compressive strength of concrete at early ages.</p> <p>For destructive evaluation, standard cylinder compression tests, splitting tensile tests and pull-out tests were made on specimens cured at 73 °F (22.8 °C), 55 °F (12.8 °C) and 35 °F (1.7 °C). For non-destructive evaluation, both probe penetration and rebound hammer tests were performed on slabs. Tests were carried out at the age of 1, 2, 3, 5, 7, 14, 28 and 42 days after casting the concrete.</p> <p>Statistical analyses were made to examine the possibility of using maturity of concrete as a parameter to correlate test results of concrete cured at different temperatures. Rate of gain of the splitting tensile strength, pull-out bond strength and elastic modulus were compared with that of compressive strength.</p> <p>The results show that when related to maturity, the rate of increase in the splitting tensile strength is about the same as that of the compressive strength, whereas the rate of increase in the pull-out strength and the modulus are slightly greater than that of the compressive strength. The results of non-destructive evaluations revealed that the compressive strength could not be estimated correctly by the probe method using the manufacturer's conversion charts. Because of lower rebound readings, the rebound hammer could not be used to estimate the compressive strength at early ages.</p>			
17. KEY WORDS (six to twelve entries; alphabetical order; capitalize only the first letter of the first key word unless a proper name; separated by semicolons) Compressive strength; concrete; maturity; mechanical properties; non-destructive evaluation; pull-out strength; splitting tensile strength.			
18. AVAILABILITY <input checked="" type="checkbox"/> Unlimited  <input type="checkbox"/> For Official Distribution. Do Not Release to NTIS  <input checked="" type="checkbox"/> Order From Sup. of Doc., U.S. Government Printing Office Washington, D.C. 20402, SD Cat. No. C13.46:932  <input type="checkbox"/> Order From National Technical Information Service (NTIS) Springfield, Virginia 22151	19. SECURITY CLASS (THIS REPORT)  UNCLASSIFIED  20. SECURITY CLASS (THIS PAGE)  UNCLASSIFIED	21. NO. OF PAGES  56	22. Price  \$1.35

Get  
a line on  
science and  
technology.  
Subscribe to

# DIMENSIONS



Whether you're in business, or a teacher, scientist, or consumer, you'll want to keep up with the latest developments in science and technology. DIMENSIONS/NBS, the monthly magazine from the Commerce Department's National Bureau of Standards, can help keep you informed. Every day at NBS, one of the nation's largest research laboratories, scientists seek new answers to a host of national problems, including energy conservation, product safety, metric conversion, and pollution abatement. Their findings, reported each month in DIMENSIONS/NBS, have a direct impact on our daily lives.

Subscription price: \$9.45 per year.  
Order prepaid from the  
Superintendent of Documents,  
U.S. Government Printing Office,  
Washington, D.C. 20402  
SD Catalog No. C13

## PERIODICALS

**JOURNAL OF RESEARCH** reports National Bureau of Standards research and development in physics, mathematics, and chemistry. It is published in two sections, available separately:

• **Physics and Chemistry (Section A)**

Papers of interest primarily to scientists working in these fields. This section covers a broad range of physical and chemical research, with major emphasis on standards of physical measurement, fundamental constants, and properties of matter. Issued six times a year. Annual subscription: Domestic, \$17.00; Foreign, \$21.25.

• **Mathematical Sciences (Section B)**

Studies and compilations designed mainly for the mathematician and theoretical physicist. Topics in mathematical statistics, theory of experiment design, numerical analysis, theoretical physics and chemistry, logical design and programming of computers and computer systems. Short numerical tables. Issued quarterly. Annual subscription: Domestic, \$9.00; Foreign, \$11.25.

**DIMENSIONS/NBS (formerly Technical News Bulletin)**—This monthly magazine is published to inform scientists, engineers, businessmen, industry, teachers, students, and consumers of the latest advances in science and technology, with primary emphasis on the work at NBS. The magazine highlights and reviews such issues as energy research, fire protection, building technology, metric conversion, pollution abatement, health and safety, and consumer product performance. In addition, it reports the results of Bureau programs in measurement standards and techniques, properties of matter and materials, engineering standards and services, instrumentation, and automatic data processing.

Annual subscription: Domestic, \$9.45; Foreign, \$11.85.

## NONPERIODICALS

**Monographs**—Major contributions to the technical literature on various subjects related to the Bureau's scientific and technical activities.

**Handbooks**—Recommended codes of engineering and industrial practice (including safety codes) developed in cooperation with interested industries, professional organizations, and regulatory bodies.

**Special Publications**—Include proceedings of conferences sponsored by NBS, NBS annual reports, and other special publications appropriate to this grouping such as wall charts, pocket cards, and bibliographies.

**Applied Mathematics Series**—Mathematical tables, manuals, and studies of special interest to physicists, engineers, chemists, biologists, mathematicians, computer programmers, and others engaged in scientific and technical work.

**National Standard Reference Data Series**—Provides quantitative data on the physical and chemical properties of materials, compiled from the world's literature and critically evaluated. Developed under a world-wide program coordinated by NBS. Program under authority of National Standard Data Act (Public Law 90-396).

## BIBLIOGRAPHIC SUBSCRIPTION SERVICES

The following current-awareness and literature-survey bibliographies are issued periodically by the Bureau:

**Cryogenic Data Center Current Awareness Service.** A literature survey issued biweekly. Annual subscription: Domestic, \$20.00; Foreign, \$25.00.

**Liquified Natural Gas.** A literature survey issued quarterly. Annual subscription: \$20.00.

**NOTE:** At present the principal publication outlet for these data is the *Journal of Physical and Chemical Reference Data (JPCRD)* published quarterly for NBS by the American Chemical Society (ACS) and the American Institute of Physics (AIP). Subscriptions, reprints, and supplements available from ACS, 1155 Sixteenth St. N.W., Wash. D. C. 20056.

**Building Science Series**—Disseminates technical information developed at the Bureau on building materials, components, systems, and whole structures. The series presents research results, test methods, and performance criteria related to the structural and environmental functions and the durability and safety characteristics of building elements and systems.

**Technical Notes**—Studies or reports which are complete in themselves but restrictive in their treatment of a subject. Analogous to monographs but not so comprehensive in scope or definitive in treatment of the subject area. Often serve as a vehicle for final reports of work performed at NBS under the sponsorship of other government agencies.

**Voluntary Product Standards**—Developed under procedures published by the Department of Commerce in Part 10, Title 15, of the Code of Federal Regulations. The purpose of the standards is to establish nationally recognized requirements for products, and to provide all concerned interests with a basis for common understanding of the characteristics of the products. NBS administers this program as a supplement to the activities of the private sector standardizing organizations.

**Consumer Information Series**—Practical information, based on NBS research and experience, covering areas of interest to the consumer. Easily understandable language and illustrations provide useful background knowledge for shopping in today's technological marketplace.

*Order above NBS publications from: Superintendent of Documents, Government Printing Office, Washington, D.C. 20402.*

*Order following NBS publications—NBSIR's and FIPS from the National Technical Information Services, Springfield, Va. 22161.*

**Federal Information Processing Standards Publications (FIPS PUBS)**—Publications in this series collectively constitute the Federal Information Processing Standards Register. Register serves as the official source of information in the Federal Government regarding standards issued by NBS pursuant to the Federal Property and Administrative Services Act of 1949 as amended, Public Law 89-306 (79 Stat. 1127), and as implemented by Executive Order 11717 (38 FR 12315, dated May 11, 1973) and Part 6 of Title 15 CFR (Code of Federal Regulations).

**NBS Interagency Reports (NBSIR)**—A special series of interim or final reports on work performed by NBS for outside sponsors (both government and non-government). In general, initial distribution is handled by the sponsor; public distribution is by the National Technical Information Services (Springfield, Va. 22161) in paper copy or microfiche form.

**Superconducting Devices and Materials.** A literature survey issued quarterly. Annual subscription: \$20.00. Send subscription orders and remittances for the preceding bibliographic services to National Bureau of Standards, Cryogenic Data Center (275.02) Boulder, Colorado 80302.

**U.S. DEPARTMENT OF COMMERCE**  
**National Bureau of Standards**  
Washington, D.C. 20234

OFFICIAL BUSINESS

Penalty for Private Use, \$300

POSTAGE AND FEES PAID  
U.S. DEPARTMENT OF COMMERCE  
COM-215



SPECIAL FOURTH-CLASS RATE  
BOOK



**75 YEARS**  
**NBS**  
1901-1976