AUTHENTICATED
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INFORMATION
GPO

National banks and federal branches and federal agencies of foreign banks

District office of the Office of the Comptroller of the Currency for the district in which the institution is located.

State member banks, branches and agencies of foreign banks (other than federal branches, federal agencies, and insured state branches of foreign banks), commercial lending companies owned or controlled by foreign banks, and organizations operating under section 25 or 25A of the Federal Reserve Act

Federal Reserve Bank serving the district in which the institution is located.

Non-member insured banks and insured state branches of foreign banks

Federal Deposit Insurance Corporation Regional director for the region in which the institution is located.

SAVINGS INSTITUTIONS INSURED UNDER THE SAVINGS ASSOCIATION INSURANCE FUND OF THE FDIC AND FEDERALLY CHARTERED SAVINGS BANKS INSURED UNDER THE BANK INSURANCE FUND OF THE FDIC (BUT NOT INCLUDING STATE-CHARTERED SAVINGS BANKS INSURED UNDER THE BANK INSURANCE FUND).

Office of Thrift Supervision Regional Director for the region in which the institution is located.

FEDERAL CREDIT UNIONS

Regional office of the National Credit Union Administration serving the area in which the Federal credit union is located.

AIR CARRIERS

Assistant General Counsel for Aviation Enforcement and Proceedings, Department of Transportation, 400 Seventh Street, SW., Washington, DC 20590.

CREDITORS SUBJECT TO PACKERS AND STOCKYARDS ACT

Nearest Packers and Stockyards Administration area supervisor.

FEDERAL LAND BANKS, FEDERAL LAND BANK ASSOCIATIONS, FEDERAL INTERMEDIATE CREDIT BANKS AND PRODUCTION CREDIT ASSOCIATIONS.

Farm Credit Administration, 490 L'Enfant Plaza, SW., Washington, DC 20578.

RETAIL, DEPARTMENT STORES, CONSUMER FINANCE COMPANIES, ALL OTHER CREDITORS, AND ALL NONBANK CREDIT CARD ISSUERS (CREDITORS OPERATING ON A LOCAL OR REGIONAL BASIS SHOULD USE THE ADDRESS OF THE FTC REGIONAL OFFICE IN WHICH THEY OPERATE.)

Division of Credit Practices, Bureau of Consumer Protection, Federal Trade Commission, Washington, DC 20580.

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APPENDIX J TO PART 226—ANNUAL PERCENTAGE RATE COMPUTATIONS FOR CLOSED-END CREDIT TRANSACTIONS

(A) INTRODUCTION

(1) Section 226.22(a) of Regulation Z provides that the annual percentage rate for other than open end credit transactions shall be determined in accordance with either the actuarial method or the United States Rule method. This appendix contains an explanation of the actuarial method as well as equations, instructions and examples of how this method applies to single advance and multiple advance transactions.

(2) Under the actuarial method, at the end of each unit-period (or fractional unit-period) the unpaid balance of the amount financed is increased by the finance charge earned during that period and is decreased by the total payment (if any) made at the end of that period. The determination of unit-periods and fractional unit-periods shall be consistent with the definitions and rules in paragraphs (b) (3), (4) and (5) of this section and the general equation in paragraph (b)(8) of this section.

(3) In contrast, under the United States Rule method, at the end of each payment period, the unpaid balance of the amount financed is increased by the finance charge earned during that payment period and is decreased by the payment made at the end of that payment period. If the payment is less than the finance charge earned, the adjustment of the unpaid balance of the amount financed is postponed until the end of the next payment period. If at that time the sum of the two payments is still less than the total earned finance charge for the two payment periods, the adjustment of the unpaid balance of the amount financed is postponed still another payment period, and so forth.

(B) INSTRUCTIONS AND EQUATIONS FOR THE ACTUARIAL METHOD

(1) General Rule

The annual percentage rate shall be the nominal annual percentage rate determined

by multiplying the unit-period rate by the number of unit-periods in a year.

(2) Term of the Transaction

The term of the transaction begins on the date of its consummation, except that if the finance charge or any portion of it is earned beginning on a later date, the term begins on the later date. The term ends on the date the last payment is due, except that if an advance is scheduled after that date, the term ends on the later date. For computation purposes, the length of the term shall be equal to the time interval between any point in time on the beginning date to the same point in time on the ending date.

(3) Definitions of Time Intervals

(i) A period is the interval of time between advances or between payments and includes the interval of time between the date the finance charge begins to be earned and the date of the first advance thereafter or the date of the first payment thereafter, as applicable.

(ii) A common period is any period that occurs more than once in a transaction.

(iii) A standard interval of time is a day, week, semimonth, month, or a multiple of a week or a month up to, but not exceeding, 1 year.

(iv) All months shall be considered equal. Full months shall be measured from any point in time on a given date of a given month to the same point in time on the same date of another month. If a series of payments (or advances) is scheduled for the last day of each month, months shall be measured from the last day of the given month to the last day of another month. If payments (or advances) are scheduled for the 29th or 30th of each month, the last day of February shall be used when applicable.

(4) Unit-period

(i) In all transactions other than a single advance, single payment transaction, the unit-period shall be that common period, not to exceed 1 year, that occurs most frequently in the transaction, except that

(A) If 2 or more common periods occur with equal frequency, the smaller of such common periods shall be the unit-period; or

(B) If there is no common period in the transaction, the unit-period shall be that period which is the average of all periods rounded to the nearest whole standard interval of time. If the average is equally near 2 standard intervals of time, the lower shall be the unit-period.

(ii) In a single advance, single payment transaction, the unit-period shall be the term of the transaction, but shall not exceed 1 year.

(5) Number of Unit-periods Between 2 Given Dates

(i) The number of days between 2 dates shall be the number of 24-hour intervals between any point in time on the first date to the same point in time on the second date.

(ii) If the unit-period is a month, the number of full unit-periods between 2 dates shall be the number of months measured back from the later date. The remaining fraction of a unit-period shall be the number of days measured forward from the earlier date to the beginning of the first full unit-period, divided by 30. If the unit-period is a month, there are 12 unit-periods per year.

(iii) If the unit-period is a semimonth or a multiple of a month not exceeding 11 months, the number of days between 2 dates shall be 30 times the number of full months measured back from the later date, plus the number of remaining days. The number of full unit-periods and the remaining fraction of a unit-period shall be determined by dividing such number of days by 15 in the case of a semimonthly unit-period or by the appropriate multiple of 30 in the case of a multimonthly unit-period. If the unit-period is a semimonth, the number of unit-periods per year shall be 24. If the number of unit-periods is a multiple of a month, the number of unit-periods per year shall be 12 divided by the number of months per unit-period.

(iv) If the unit-period is a day, a week, or a multiple of a week, the number of full unit-periods and the remaining fractions of a unit-period shall be determined by dividing the number of days between the 2 given dates by the number of days per unit-period. If the unit-period is a day, the number of unit-periods per year shall be 365. If the unit-period is a week or a multiple of a week, the number of unit-periods per year shall be 52 divided by the number of weeks per unit-period.

(v) If the unit-period is a year, the number of full unit-periods between 2 dates shall be the number of full years (each equal to 12 months) measured back from the later date. The remaining fraction of a unit-period shall be

(A) The remaining number of months divided by 12 if the remaining interval is equal to a whole number of months, or

(B) The remaining number of days divided by 365 if the remaining interval is *not* equal to a whole number of months.

(vi) In a single advance, single payment transaction in which the term is less than a year and is equal to a whole number of months, the number of unit-periods in the term shall be 1, and the number of unit-periods per year shall be 12 divided by the number of months in the term or 365 divided by the number of days in the term.

(vii) In a single advance, single payment transaction in which the term is less than a year and is *not* equal to a whole number of

months, the number of unit-periods in the term shall be 1, and the number of unit-periods per year shall be 365 divided by the number of days in the term.

(6) Percentage Rate for a Fraction of a Unit-period

The percentage rate of finance charge for a fraction (less than 1) of a unit-period shall be equal to such fraction multiplied by the percentage rate of finance charge per unit-period.

(7) Symbols. The symbols used to express the terms of a transaction in the equation set forth in paragraph (b)(8) of this section are defined as follows:

A_k = The amount of the kth advance.

q_k = The number of full unit-periods from the beginning of the term of the transaction to the kth advance.

e_k = The fraction of a unit-period in the time interval from the beginning of the term of the transaction to the kth advance.

m = The number of advances.

P_j = The amount of the jth payment.

t_j = The number of full unit-periods from the beginning of the term of the transaction to the jth payment.

f_j = The fraction of a unit-period in the time interval from the beginning of the term of the transaction to the jth payment.

n = The number of payments.

i = The percentage rate of finance charge per unit-period, expressed as a decimal equivalent.

Symbols used in the examples shown in this appendix are defined as follows:

$\ddot{a}_{\overline{x}|}$ = The present value of 1 per unit-period for x unit-periods, first payment due immediately.

$$= 1 + \frac{1}{(1+i)} + \frac{1}{(1+i)^2} + \ldots\ldots\ldots + \frac{1}{(1+i)^{x-1}}$$

w = The number of unit-periods per year.

I = wi x 100 = The nominal annual percentage rate.

(8) General equation. The following equation sets forth the relationship among the terms of a transaction:

$$\frac{A_1}{(1+e_1 i)(1+i)_1^{q}} + \frac{A_2}{(1+e_2 i)(1+i)_2^{q}} + \cdots + \frac{A_m}{(1+e_m i)(1+i)_m^{q}} =$$

$$\frac{P_1}{(1+f_1 i)(1+i)_1^{t}} + \frac{P_2}{(1+f_2 i)(1+i)_2^{t}} + \cdots + \frac{P_n}{(1+f_n i)(1+i)_n^{t}}$$

(9) Solution of general equation by iteration process. (i) The general equation in paragraph (b)(8) of this section, when applied to a simple transaction in which a loan of $1000 is repaid by 36 monthly payments of $33.61 each, takes the special form:

$$A = \frac{33.61\ \ddot{a}_{\overline{36}|}}{(1+i)}$$

Step 1: Let I_1 = estimated annual percentage rate = 12.50 %

Evaluate expression for A, letting $i = I_1/(100w)$ = .010416667

Result (referred to as A')= 1004.674391

Step 2: Let $I_2 = I_1 + .1$ = 12.60 %

Evaluate expression for A, letting $i = I_2/(100w)$ = .010500000

Result (referred to as A'') = 1003.235366

Step 3: Interpolate for I (annual percentage rate):

$$I = I_1 + .1\left[\frac{(A - A')}{(A''-A')}\right]$$

$$= 12.50 + .1\left[\frac{(1000.000000 - 1004.674391)}{(1003.235366 - 1004.674391)}\right] = 12.82483042\ \%$$

Step 4: First iteration, let I_1 = 12.82483042 % and repeat Steps 1, 2, and 3 obtaining a new I = 12.82557859 %

Second iteration, let I_1 = 12.82557859 % and repeat Steps 1, 2, and 3 obtaining a new I = 12.82557529 %

In this case, no further iterations are required to obtain the annual percentage rate correct to two decimal places, 12.83%.

(ii) When the iteration approach is used, it is expected that calculators or computers will be programmed to carry all available decimals throughout the calculation and that enough iterations will be performed to make virtually certain that the annual percentage rate obtained, when rounded to 2 decimals, is correct. Annual percentage rates in the examples below were obtained by using a 10 digit programmable calculator and the iteration procedure described above.

(c) Examples for the actuarial method. (1) Single advance transaction, with or without an odd first period, and otherwise regular. The general equation in paragraph (b)(8) of this section can be put in the following special form for this type of transaction:

$$A = \frac{1}{(1+fi)(1+i)^{t}} \left(P \, \ddot{a}_{\overline{n}|} \right)$$

Example (i): Monthly payments (regular first period)

Amount advanced (A) = $5000. Payment (P) = $230.
Number of payments (n) = 24.
Unit-period = 1 month. Unit-periods per year (w) = 12.
Advance, 1-10-78. First payment, 2-10-78.
From 1-10-78 through 2-10-78 = 1 unit-period. (t = 1; f= 0)
Annual percentage rate (I) = wi = .0969 = 9.69 %

Example (ii): Monthly payments (long first period)

Amount advanced (A) = $6000. Payment (P) = $200.
Number of payments (n) = 36.
Unit-period = 1 month. Unit-periods per year (w) = 12.
Advance, 2-10-78. First payment, 4-1-78.
From 3-1-78 through 4-1-78 = 1 unit-period. (t = 1)
From 2-10-78 through 3-1-78 = 19 days. (f = 19/30)
Annual percentage rate (I) = wi = .1182 = 11.82%

Example (iii): Semimonthly payments (short first period)

Amount advanced (A) = $5000. Payment (P) = $219.17.
Number of payments (n) = 24.
Unit-period = 1/2 month. Unit-periods per year (w) = 24.
Advance, 2-23-78. First payment, 3-1-78. Payments made on 1st and 16th of each month.
From 2-23-78 through 3-1-78 = 6 days. (t = 0; f = 6/15)
Annual percentage rate (I) = wi = .1034 = 10.34 %

Example (iv): Quarterly payments (long first period)

Amount advanced (A) = $10,000. Payment (P) = $385.
Number of payments (n) = 40.
Unit-period = 3 months. Unit-periods per year (w) = 4.
Advance, 5-23-78. First payment, 10-1-78.
From 7-1-78 through 10-1-78 = 1 unit-period. (t = 1)
From 6-1-78 through 7-1-78 = 1 month = 30 days. From 5-23-78 through 6-1-78 = 9 days. (f = 39/90)
Annual percentage rate (I) = wi = .0897 = 8.97 %

Example (v): Weekly payments (long first period)

Amount advanced (A) = $500. Payment (P) = $17.60.
Number of payments (n) = 30.
Unit-period = 1 week. Unit-periods per year (w) = 52.
Advance, 3-20-78. First payment, 4-21-78.
From 3-24-78 through 4-21-78 = 4 unit-periods. (t = 4)
From 3-20-78 through 3-24-78 = 4 days. (f = 4/7)
Annual percentage rate (I) = wi = .1496 = 14.96 %

(2) Single advance transaction, with an odd first payment, with or without an odd first period, and otherwise regular. The general equation in paragraph (b)(8) of this section can be put in the following special form for this type of transaction:

$$A = \frac{1}{(1+fi)(1+i)^{t}} \left[P_1 + \frac{P\,\ddot{a}_{\overline{n-1}|}}{(1+i)} \right]$$

Example (i): Monthly payments (regular first period and irregular first payment)

Amount advanced (A) = $5000. First payment $\left(P_1\right)$ = $250.
Regular payment (P) = $230. Number of payments (n) = 24.
Unit-period = 1 month. Unit-periods per year (w) = 12.
Advance, 1-10-78. First payment, 2-10-78.
From 1-10-78 through 2-10-78 = 1 unit-period. (t = 1; f = 0)
Annual percentage rate (I) = wi = .1008 = 10.08%

Example (ii): Payments every 4 weeks (long first period and irregular first payment)

Amount advanced (A) = $400. First payment $\left(P_1\right)$ = $39.50.
Regular payment (P) = $38.31. Number of payments (n) = 12.
Unit-period = 4 weeks. Unit-periods per year (w) = 52/4 = 13.
Advance, 3-18-78. First payment, 4-20-78.
From 3-23-78 through 4-20-78 = 1 unit-period. (t = 1)
From 3-18-78 through 3-23-78 = 5 days. (f = 5/28)
Annual percentage rate (I) = wi = .2850 = 28.50%

(3) Single advance transaction, with an odd final payment, with or without an odd first period, and otherwise regular. The general equation in paragraph (b)(8) of this section can be put in the following special form for this type of transaction:

$$A = \frac{1}{(1+fi)(1+i)^{t}} \left[P\,\ddot{a}_{\overline{n-1}|} + \frac{Pn}{(1+i)^{n-1}} \right]$$

Example (i): Monthly payments (regular first period and irregular final payment)

Amount advanced (A) = $5000. Regular payment (P) = $230.
Final payment $\left(\begin{matrix} P \\ n \end{matrix}\right)$ = $280. Number of payments (n) = 24.
Unit-period = 1 month. Unit-periods per year (w) = 12.
Advance, 1-10-78. First payment, 2-10-78.
From 1-10-78 through 2-10-78 = 1 unit-period. (t = 1; f = 0)
Annual percentage rate (I) = wi = .1050 = 10.50%

Example (ii): Payments every 2 weeks (short first period and irregular final payment)

Amount advanced (A) = $200. Regular payment (P) = $9.50.
Final payment $\left(\begin{matrix} P \\ n \end{matrix}\right)$ = $30. Number of payments (n) = 20.
Unit-period = 2 weeks. Unit-periods per year (w) = 52/2 = 26.
Advance, 4-3-78. First payment, 4-11-78.
From 4-3-78 through 4-11-78 = 8 days. (t = 0; f = 8/14)
Annual percentage rate (I) = wi = .1222 = 12.22%

(4) Single advance transaction, with an odd first payment, odd final payment, with or without an odd first period, and otherwise regular. The general equation in paragraph (b)(8) of this section can be put in the following special form for this type of transaction:

$$A = \frac{1}{(1+fi)(1+i)^{t}} \left[P_1 + \frac{P \ddot{a}_{\overline{n-2}|}}{(1+i)} + \frac{P_n}{(1+i)^{n-1}} \right]$$

Example (i): Monthly payments (regular first period, irregular first payment, and irregular final payment)

Amount advanced (A) = $5000. First payment $\left(\begin{matrix} P \\ 1 \end{matrix}\right)$ = $250.
Regular payment (P) = $230. Final payment $\left(\begin{matrix} P \\ n \end{matrix}\right)$ = $280.
Number of payments (n) = 24. Unit-period = 1 month.
Unit-periods per year (w) = 12.
Advance, 1-10-78. First payment, 2-10-78.
From 1-10-78 through 2-10-78 = 1 unit-period. (t = 1; f = 0)
Annual percentage rate (I) = wi = .1090 = 10.90%

Example (ii): Payments every two months (short first period, irregular first payment, and irregular final payment)

Amount advanced (A) = $8000. First payment $\left(\begin{matrix} P \\ 1 \end{matrix}\right)$ = $449.36.
Regular payment (P) = $465. Final payment $\left(\begin{matrix} P \\ n \end{matrix}\right)$ = $200.
Number of payments (n) = 20. Unit-period = 2 months.
Unit-periods per year (w) = 12/2 = 6.
Advance, 1-10-78. First payment, 3-1-78.
From 2-1-78 through 3-1-78 = 1 month. From 1-10-78 through 2-1-78 = 22 days. (t = 0; f = 52/60)
Annual percentage rate (I) = wi = .0730 = 7.30%

(5) Single advance, single payment transaction. The general equation in paragraph (b)(8) of this section can be put in the special forms below for single advance, single payment transactions. Forms 1 through 3 are for the direct determination of the annual percentage rate under special conditions. Form 4 requires the use of the iteration procedure of paragraph (b)(9) of this section and can be used for all single advance, single payment transactions regardless of term.

Form 1 - Term less than 1 year:

$$I = 100w\left(\frac{P}{A} - 1\right)$$

Form 2 - Term more than 1 year but less than 2 years:

$$I = \frac{50}{f}\left\{\left[(1 + f)^2 + 4f\left(\frac{P}{A} - 1\right)\right]^{1/2} - (1 + f)\right\}$$

Form 3 - Term equal to exactly a year or exact multiple of a year:

$$I = 100\left[\left(\frac{P}{A}\right)^{1/t} - 1\right]$$

Form 4 - Special form for iteration procedure (no restriction on term):

$$A = \frac{P}{(1 + fi)(1 + i)^t}$$

Example (i): Single advance, single payment (term of less than 1 year, measured in days)

Amount advanced (A) = $1000. Payment (P) = $1080.
Unit-period = 255 days. Unit-periods per year (w) = 365/255.
Advance, 1-3-78. Payment, 9-15-78.
From 1-3-78 through 9-15-78 = 255 days. (t = 1; f = 0)
Annual percentage rate (I) = wi = .1145 = 11.45%. (Use Form 1 or 4.)

Example (ii): Single advance, single payment (term of less than 1 year, measured in exact calendar months)

Amount advanced (A) = $1000. Payment (P) = $1044.
Unit-period = 6 months. Unit-periods per year (w) = 2.
Advance, 7-15-78. Payment, 1-15-79.
From 7-15-78 through 1-15-79 = 6 mos. (t = 1; f = 0)
Annual percentage rate (I) = wi = .0880 = 8.80%. (Use Form 1 or 4.)

Example (iii): Single advance, single payment (term of more than 1 year but less than 2 years, fraction measured in exact months)

Amount advanced (A) = $1000. Payment (P) = $1135.19.
Unit-period = 1 year. Unit-periods per year (w) = 1.
Advance, 7-17-78. Payment, 1-17-80.
From 1-17-79 through 1-17-80 = 1 unit-period. (t = 1)
From 7-17-78 through 1-17-79 = 6 mos. (f = 6/12)
Annual percentage rate (I) = wi = .0876 = 8.76%. (Use Form 2 or 4.)

Example (iv): Single advance, single payment (term of exactly 2 years)

Amount advanced (A) = $1000. Payment (P) = $1240.
Unit-period = 1 year. Unit-periods per year (w) = 1.
Advance, 1-3-78. Payment, 1-3-80.
From 1-3-78 through 1-3-79 = 1 unit-period. (t = 2; f = 0)
Annual percentage rate (I) = wi = .1136 = 11.36%. (Use Form 3 or 4.)

(6) Complex single advance transaction.

Example (i): Skipped payment loan (payments every 4 weeks)

A loan of $2135 is advanced on 1-25-78. It is to be repaid by 24 payments of $100 each. Payments are due every 4 weeks beginning 2-20-78. However, in those months in which 2 payments would be due, only the first of the 2 payments is made and the following payment is delayed by 2 weeks to place it in the next month.
Unit-period = 4 weeks. Unit-periods per year (w) = 52/4 = 13.
First series of payments begins 26 days after 1-25-78.
(t = 0; f = 26/28)
1 1

Second series of payments begins 9 unit-periods plus 2 weeks after start of first series. (t = 10; f = 12/28)
2 2

Third series of payments begins 6 unit-periods plus 2 weeks after start of second series. (t = 16; f = 26/28)
3 3

Last series of payments begins 6 unit-periods plus 2 weeks after start of third series. (t = 23; f = 12/28)
4 4

The general equation in paragraph (b)(8) of this section can be written in the special form:

$$2135 = \frac{100\ \ddot{a}_{\overline{9}|}}{(1+(26/28)i)} + \frac{100\ \ddot{a}_{\overline{6}|}}{(1+(12/28)i)(1+i)^{10}} + \frac{100\ \ddot{a}_{\overline{6}|}}{(1+(26/28)i)(1+i)^{16}} + \frac{100\ \ddot{a}_{\overline{3}|}}{(1+(12/28)i)(1+i)^{23}}$$

Annual percentage rate (I) = wi = .1200 = 12.00%

Example (ii): Skipped payment loan plus single payments

A loan of $7350 on 3-3-78 is to be repaid by 3 monthly payments of $1000 each beginning 9-15-78, plus a single payment of $2000 on 3-15-79, plus 3 more monthly payments of $750 each beginning 9-15-79, plus a final payment of $1000 on 2-1-80. Unit-period = 1 month. Unit-periods per year (w) = 12. First series of payments begins 6 unit-periods plus 12 days after 3-3-78. ($t_1 = 6$; $f_1 = 12/30$)

Second series of payments (single payment) occurs 12 unit-periods plus 12 days after 3-3-78. ($t_2 = 12$; $f_2 = 12/30$)

Third series of payments begins 18 unit-periods plus 12 days after 3-3-78. ($t_3 = 18$; $f_3 = 12/30$)

Final payment occurs 22 unit-periods plus 29 days after 3-3-78. ($t_4 = 22$; $f_4 = 29/30$)

The general equation in paragraph (b)(8) of this section can be written in the special form:

$$7350 = \frac{1000\ \ddot{a}_{\overline{3}|}}{(1+(12/30)i)(1+i)^{6}} + \frac{2000}{(1+(12/30)i)(1+i)^{12}} + \frac{750\ \ddot{a}_{\overline{3}|}}{(1+(12/30)i)(1+i)^{18}} + \frac{1000}{(1+(29/30)i)(1+i)^{22}}$$

Annual percentage rate (I) = wi = .1022 = 10.22%

Example (iii): Mortgage with varying payments

A loan of $39,688.56 (net) on 4-10-78 is to be repaid by 360 monthly payments beginning 6-1-78. Payments are the same for 12 months at a time as follows:

Year	Monthly payment	Year	Monthly payment	Year	Monthly payment
1	$291.81	11	$385.76	21	$380.43
2	300.18	12	385.42	22	379.60
3	308.78	13	385.03	23	378.68
4	317.61	14	384.62	24	377.69
5	326.65	15	384.17	25	376.60
6	335.92	16	383.67	26	375.42
7	345.42	17	383.13	27	374.13
8	355.15	18	382.54	28	372.72
9	365.12	19	381.90	29	371.18
10	375.33	20	381.20	30	369.50

Unit-period = 1 month. Unit-periods per year (w) = 12.
From 5-1-78 through 6-1-78 = 1 unit-period. (t = 1)
From 4-10-78 through 5-1-78 = 21 days. (f = 21/30)

The general equation in paragraph (b)(8) of this section can be written in the special form:

$$39{,}688.56 = \frac{\ddot{a}_{\overline{12}|}}{(1+(21/30)i)(1+i)} \left[291.81 + \frac{300.18}{(1+i)^{12}} + \frac{308.78}{(1+i)^{24}} + \ldots + \frac{369.50}{(1+i)^{348}} \right]$$

Annual percentage rate (I) = wi = .0980 = 9.80%

(7) Multiple advance transactions.

Example (i): Construction loan

Three advances of $20,000 each are made on 4-10-79, 6-12-79, and 9-18-79. Repayment is by 240 monthly payments of $612.36 each beginning 12-10-79.
Unit-period = 1 month. Unit-periods per year (w) = 12.
From 4-10-79 through 6-12-79 = (2+2/30) unit-periods.
From 4-10-79 through 9-18-79 = (5+8/30) unit-periods.
From 4-10-79 through 12-10-79 = (8) unit-periods.

The general equation in paragraph (b)(8) of this section is changed to the single advance mode by treating the 2nd and 3rd advances as negative payments:

$$20{,}000 = \frac{612.36\ \ddot{a}_{\overline{240}|}}{(1+i)^{8}} - \frac{20{,}000}{(1+(2/30)i)(1+i)^{2}} - \frac{20{,}000}{(1+(8/30)i)(1+i)^{5}}$$

Annual percentage rate (I) = wi = .1025 = 10.25%

Example (ii): Student loan

A student loan consists of 8 advances: $1800 on 9-5-78, 9-5-79, 9-5-80, and 9-5-81; plus $1000 on 1-5-79, 1-5-80, 1-5-81, and 1-5-82. The borrower is to make 50 monthly payments of $240 each beginning 7-1-78 (prior to first advance).
Unit-period = 1 month. Unit-periods per year (w) = 12.
Zero point is date of first payment since it precedes first advance.
From 7-1-78 to 9-5-78 = (2 + 4/30) unit-periods.

" " " 9-5-79 = (14 + 4/30) "

" " " 9-5-80 = (26 + 4/30) "

" " " 9-5-81 = (38 + 4/30) "

" " " 1-5-79 = (6 + 4/30) "

" " " 1-5-80 = (18 + 4/30) "

" " " 1-5-81 = (30 + 4/30) "

" " " 1-5-82 = (42 + 4/30) "

Since the zero point is date of first payment, the general equation in paragraph (b)(8) of this section is written in the single advance form below by treating the first payment as a negative advance and the 8 advances as negative payments:

$$-240 = \frac{240\ \ddot{a}_{\overline{49}|}}{(1+i)} - \frac{1800}{(1+(4/30)i)}\left[\frac{1}{(1+i)^{2}} + \frac{1}{(1+i)^{14}} + \frac{1}{(1+i)^{26}} + \frac{1}{(1+i)^{38}}\right] - \frac{1000}{(1+(4/30)i)}\left[\frac{1}{(1+i)^{6}} + \frac{1}{(1+i)^{18}} + \frac{1}{(1+i)^{30}} + \frac{1}{(1+i)^{42}}\right]$$

Annual percentage rate (I) = wi = .3204 = 32.04%

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